

Central Rockies Variant  
Of the  
Forest Vegetation Simulator

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## 1.0 INTRODUCTION

The Forest Vegetation Simulator (FVS) is an individual tree, distance independent growth and yield model with linkable modules, called extensions, which simulate various insect and pathogen impacts, fire effects, fuel loading, snag dynamics, and development of understory vegetation. The FVS model was originally called Prognosis (Stage, 1973) and was developed for use in the Inland Empire area of Idaho and Montana. New “variants” of the FVS model are created by imbedding new tree growth, mortality, and volume equations for a particular geographic area in the FVS framework. Geographic variants of FVS have been developed for most of the forested lands in the western, upper mid-west, northeast, and some areas of the southeast United States. FVS can simulate a wide variety of forest types, stand structures, and pure or mixed species stands.

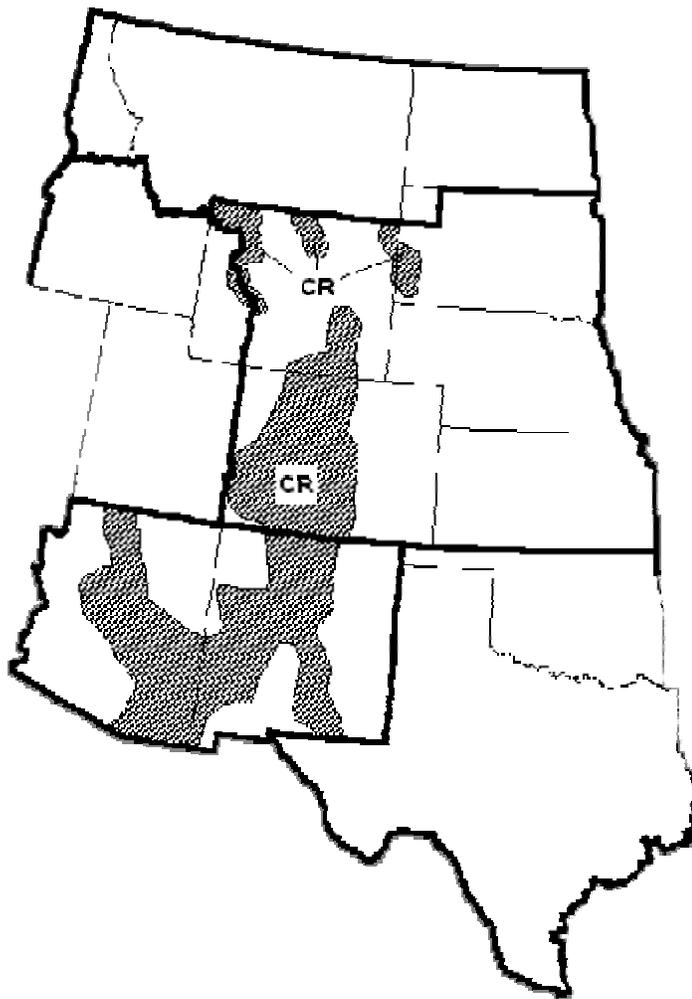
The Central Rockies (CR) variant of FVS was originally developed in 1990. It was based on the growth equations and relationships from the GENGYM model (Edminster, Mowrer, Mathiasen, et. al. 1991). Although GENGYM is a diameter class model, and FVS is an individual tree model, results produced with FVS were consistent with those produced by GENGYM. While general model upgrades, enhancements, and error fixes, were made to the code since 1990, the variant essentially remained the same as when it was developed.

In late 1998, staff at the Forest Management Service Center began a major overhaul of the variant to correct known deficiencies and quirks, take advantage of advances in FVS technology, incorporate additional data into certain model relationships, and improve default values and surrogate species assignments. In addition, the model was expanded to include 24 species and allow all National Forests within the geographic range of the model to access all the imbedded model types.

## 2.0 GEOGRAPHIC RANGE

The CR variant covers all the National Forests in Regions 2 and 3. It extends from the northern border of Wyoming, down through Colorado, and into Arizona and New Mexico. However, given the changes that have taken place in this major upgrade, the model could be applied to the forests in Utah and southern Idaho as well. A map indicating the approximate geographic area covered by this variant is shown in Figure 1.

Figure 1. Approximate geographic area covered by the Central Rockies variant of the Forest Vegetation Simulator.



### 3.0 CONTROL VARIABLES

Users should specify certain variables used by the Central Rockies variant to control the simulation. These are entered in parameter fields on various FVS keywords.

#### 3.1 MODEL TYPE

The CR variant contains the 5 model types, shown in Table 1. Model type is entered as a number, ranging from 1 to 5, in Field 1 of the MODTYPE keyword. If the MODTYPE keyword is missing, or contains an incorrect value, then the default model type is determined from the forest code. The default model type by Forest code is shown in Table 2.

Some equations, for some species, are different depending on which model type is selected. For example, ponderosa pine growth relationships are different if Black Hills is selected as the model type, as opposed to Southwestern Ponderosa Pine. For other species, such as Douglas-fir, the growth equations are the same in all model types. The abbreviation shown in the last column of Table 1 is used to identify the model type, and is also used in labeling some FVS output files.

Table 1. Model types used in the Central Rockies FVS variant:

Model Type	Description	Output Abbreviation
1	Southwestern Mixed Conifers	SM
2	Southwestern Ponderosa Pine	SP
3	Black Hills Ponderosa Pine	BP
4	Spruce-fir	SF
5	Lodgepole Pine	LP

#### 3.2 FOREST CODE AND DEFAULT MODEL TYPE

Forest code is entered as a number in Field 1 of the STDINFO keyword. Any forest code can be used with any model type code. If the forest code is missing or incorrect, a default forest code is used. If the model type is also missing or incorrect, or if the model type is 1 or 2, the default forest is 303 (Cibola National Forest); if model type 3 is specified, the default forest code is 203 (Black Hills National Forest); and if model types 4 or 5 is specified, the default forest code is 211 (Routt National Forest). A complete list of forest codes recognized in the CR variant is shown in Table 2. Forest code is used in some growth equations as an index for location effects, and to trigger the correct volume equations for that forest.

Table 2. Forest codes used in the Central Rockies FVS variant, and their associated default model types.

Forest Code	National Forest	Default Model Type
202	Bighorn	Lodgepole Pine
203	Black Hills	Black Hills Ponderosa Pine
204	Grand Mesa, Uncompahgre, Gunnison	Spruce-fir
206	Medicine Bow	Lodgepole Pine
207	Nebraska	Black Hills Ponderosa Pine
209	Rio Grande	Spruce-fir
210	Arapaho, Roosevelt	Lodgepole Pine
211	Routt	Lodgepole Pine
212	Pike, San Isabel	Spruce-fir
213	San Juan	Spruce-fir
214	Shoshone	Lodgepole Pine
215	White River	Spruce-fir

301	Apache-Sitgreaves	Southwestern Ponderosa Pine
302	Carson	Southwestern Ponderosa Pine
303	Cibola	Southwestern Ponderosa Pine
304	Coconino	Southwestern Ponderosa Pine
305	Coronado	Southwestern Ponderosa Pine
306	Gila	Southwestern Ponderosa Pine
307	Kaibab	Southwestern Ponderosa Pine
308	Lincoln	Southwestern Ponderosa Pine
309	Prescott	Southwestern Ponderosa Pine
310	Sante Fe	Southwestern Ponderosa Pine
312	Tonto	Southwestern Ponderosa Pine

### **3.3 SPECIES CODES**

The CR variant of FVS recognizes 24 species codes. These correspond to the 24 species currently output from the RMSTAND inventory program used by Forest Service Regions 2, 3, and 4 to process inventory data. Of these 24, 20 represent specific species and 4 represent the groups: “cottonwoods”, “oaks”, “other softwoods” and “other hardwoods”. Either the species alpha code or its’ Forest Inventory and Analysis (FIA) code can be used in the FVS input data. Either the species FVS number or its’ alpha code can be used to specify a species on the FVS keywords. A complete list of species codes recognized by the CR variant is shown in Table 3.

Table 3. Species codes used in the Central Rockies FVS variant.

FVS Number	Alpha Code	FIA Code	Common Name	Scientific Name
1	AF	019	Subalpine fir	<i>Abies lasiocarpa</i> var. <i>lasiocarpa</i>
2	CB	018	Corkbark fir	<i>Abies lasiocarpa</i> var. <i>arizonica</i>
3	DF	202	Douglas-fir	<i>Pseudotsuga menziesii</i>
4	GF	017	Grand fir	<i>Abies grandis</i>
5	WF	015	White fir	<i>Abies concolor</i>
6	MH	264	Mountain hemlock	<i>Tsuga mertensiana</i>
7	RC	242	Western redcedar	<i>Thuja plicata</i>
8	WL	073	Western larch	<i>Larix occidentalis</i>
9	BC	102	Bristlecone pine	<i>Pinus aristata</i>
10	LM	113	Limber pine	<i>Pinus flexilis</i> var. <i>flexilis</i>
11	LP	108	Lodgepole pine	<i>Pinus contorta</i>
12	PI	106	Pinyon pine	<i>Pinus edulis</i>
13	PP	122	Ponderosa pine	<i>Pinus ponderosa</i>
14	WB	101	Whitebark pine	<i>Pinus albicaulis</i>
15	WP	114	Southwestern white pine	<i>Pinus strobiformis</i>
16	JU	066	Rocky Mountain juniper	<i>Juniperus scopulorum</i>
17	BS	096	Blue spruce	<i>Picea pungens</i>
18	ES	093	Engelmann spruce	<i>Picea engelmannii</i>
19	WS	094	White spruce	<i>Picea glauca</i>
20	AS	746	Quaking aspen	<i>Populus tremuloides</i>
21	CO	740	Cottonwoods	<i>Populus</i> sp.
22	OA	800	Oaks	<i>Quercus</i> sp.
23	OS	001	Other softwoods	
24	OH	004	Other hardwoods	

### **3.4 SITE INDEX REFERENCES AND DEFAULTS**

The FVS CR variant uses site index as a growth predictor variable. Site index values are supplied to the model using the SITECODE keyword. If site index information is available, a single site index can be specified for the whole stand, a site index for each individual species can be specified, or a combination of these can be entered. In any event, the user should make sure the site index value being used by the model accurately portrays the productivity in the stand being projected. If the user does not supply site index values, then default values will be used. When entering site index in the CR variant, the sources shown in Table 4 should be used if possible. Default values for site species and site index, by model type, are shown in Table 5.

Table 4. Recommended site index references for use with the CR variant of FVS.

Model Type	Reference Species	Ref Age	Age Type	Reference
SW Mixed Conifers	Douglas-fir	100	Breast Height	Edminster, Mathiasen, Olsen 1991
SW Ponderosa Pine	Ponderosa pine	100	Breast Height	Minor 1964
BHills Ponderosa Pine	Ponderosa pine	100	Total	Meyer 1961
Spruce-fir	Engelmann spruce / Subalpine fir	100	Breast Height	Alexander 1967
Lodgepole Pine	Lodgepole pine	100	Total	Alexander, Tackle, Dahms 1967

Table 5. Default values for site species and site index, by model type, for the CR variant of FVS.

Model Type	Site Species	Site Index
SW Mixed Conifers	DF	70
SW Ponderosa Pine	PP	70
Bhills Ponderosa Pine	PP	57
Spruce-fir	ES	75
Lodgepole Pine	LP	65

### **3.5 STAND DENSITY INDEX DEFAULTS**

Stand Density Index (SDI) is an important variable in the mortality routine. Users can enter species-specific SDI values using the SDIMAX keyword. The SDI value is a measure of stocking and can be interpreted as the number of trees-per-acre that an area can support if all the trees were 10" in diameter. As an alternative, users can enter a basal area maximum using the BAMAX keyword, and the model will then compute a SDI maximum from the specified basal area maximum. However, this alternative is NOT recommended because a single SDI value will be applied to all species. This is not biologically correct and it also eliminates some sophistication of the mortality model (see MORTALITY section). Default SDI values for the CR variant are shown in Table 6.

Table 6. Default values for stand density index for the CR variant of FVS.

FVS Number	Alpha Code	Common Name	SDI Maximum
1	AF	Subalpine fir	735
2	CB	Corkbark fir	735
3	DF	Douglas-fir	560
4	GF	Grand fir	735
5	WF	White fir	735
6	MH	Mountain hemlock	735
7	RC	Western redcedar	770
8	WL	Western larch	650
9	BC	Bristlecone pine	470
10	LM	Limber pine	470
11	LP	Lodgepole pine	675
12	PI	Pinyon pine	415
13	PP	Ponderosa pine	529
14	WB	Whitebark pine	470
15	WP	Western white pine	645
16	JU	Western juniper	415
17	BS	Blue spruce	735
18	ES	Engelmann spruce	735
19	WS	White spruce	735
20	AS	Quaking aspen	725
21	CO	Cottonwoods	470
22	OA	Oaks	470
23	OS	Other softwoods	470
24	OH	Other hardwoods	470

### **3.6 PLANT ASSOCIATIONS**

Plant association codes are only used in the fire and fuels extension to this variant (see section 7.0), they are not used in any of the growth relationships. Users do not need to enter plant association codes if the fire and fuels extension is not being used.

Plant association codes are entered in field 2 of the STDINFO keyword. Plant association codes are used to select the appropriate default fuel model. Codes recognized in this variant are the NRIS Common Stand Exam codes (USDA Forest Service 2000), pre-pended with a one-digit Region number. Valid codes are shown in Appendices A and B. Region 2 codes originate from Johnson (1987), and Region 3 codes from USDA Forest Service (1997).

## 4.0 GROWTH MODEL RELATIONSHIPS

For discussion purposes, model relationships can be broken into groups by their function. There are those that estimate values missing in the input data; those that estimate growth on trees smaller than some threshold diameter; those that estimate growth on trees larger than some threshold diameter; those used for mortality; and those used for crown ratio change.

### 4.1 HEIGHT – DIAMETER RELATIONSHIPS

Height-diameter relationships are used for two purposes in the model: (1) to estimate heights missing in the input data, and (2) to estimate diameter growth on trees smaller than some threshold diameter. In the CR variant, height-diameter relationships are a logistic functional form, as shown in equation {1} (Wykoff, et.al 1982). The equation was fit to data of the same species used to develop other FVS variants. Default equation coefficients are shown in Table 7.

$$\{1\} \text{ HT} = 4.5 + e^{a + b(\text{DBH}+1)}$$

where HT is the total tree height in feet  
 DBH is the tree diameter at breast height  
 a, b are species specific coefficients show in Table 7

When heights are given in the input data for 3 or more trees of a given species, the value of “a” in equation {1} for that species is recalculated from the input data and replaces the default value shown in Table 7. In the event that the calculated value is less than zero, the default is used..

Table 7. Default coefficients for the CR variant height-diameter relationship

FVS Number	Alpha Code	Common Name	“a” Coefficient	“b” Coefficient
1	AF	Subalpine fir	4.4717	-6.7387
2	CB	Corkbark fir	4.4717	-6.7387
3	DF	Douglas-fir	4.5879	-8.9277
4	GF	Grand fir	5.0271	-11.2168
5	WF	White fir	4.3008	-6.8139
6	MH	Mountain hemlock	4.8740	-10.4050
7	RC	Western redcedar	5.1631	-9.2566
8	WL	Western larch	5.1631	-9.2566
9	BC	Bristlecone pine	4.1920	-5.1651
10	LM	Limber pine	4.1920	-5.1651
11	LP	Lodgepole pine	4.3767	-6.1281
12	PI	Pinyon pine	4.1920	-5.1651
13	PP	Ponderosa pine	4.6024	-11.4693
14	WB	Whitebark pine	4.1920	-5.1651
15	WP	Western white pine	5.1999	-9.2672
16	JU	Western juniper	4.1920	-5.1651
17	BS	Blue spruce	4.5293	-7.7725
18	ES	Engelmann spruce	4.5293	-7.7725
19	WS	White spruce	4.5293	-7.7725
20	AS	Quaking aspen	4.4421	-6.5405
21	CO	Cottonwoods	4.4421	-6.5405
22	OA	Oaks	4.1920	-5.1651
23	OS	Other softwoods	4.2597	-9.3949
24	OH	Other hardwoods	4.4421	-6.5405

For the Black Hills Ponderosa Pine model type, the default height-diameter relationships for all species is shown in the following equations:

$$\{2\} \text{ HT} = 32.108633 * (\text{SI}^{0.276926}) * [(1 - e^{-0.057766 * \text{DBH}})^{1.0026686}] + 4.5 \quad \text{for DBH} > 0.5''$$

$$\{3\} \text{ HT} = \text{DBH} * [12.41173 + 0.04633 * \text{SI} - 0.000158 * \text{SI}^2] \quad \text{for DBH} \leq 0.5''$$

where HT is the total tree height in feet  
 DBH is the tree diameter at breast height  
 SI is the site index for the species

However, the calibrated logistic function is used for a given species when there are enough observations to get a satisfactory estimate of the “a” parameter for that species.

## **4.2 STAGNATION EFFECT**

A stagnation effect on growth and mortality is built into the Central Rockies variant. The stagnation effect, equation {4}, is a number between 0.5 and 1.0 which indicates a proportion reduction in growth and mortality due to a stand becoming stagnated. The full stagnation effect is applied to large tree diameter growth and half the stagnation effect is applied to large tree height growth. The default condition in the variant is to not consider stagnation effects on growth. However, users can activate this feature by putting a 1 in field 7 of the SDIMAX keyword.

$$\{4\} \text{ DSTAG} = 3.33333 * (1 - \text{RELSDI}) \quad \text{for } 0.7 < \text{RELSDI} \leq 0.85$$

$$\begin{array}{ll} \text{DSTAG} = 1.0 & \text{for } \text{RELSDI} \leq 0.7 \\ \text{DSTAG} = 0.5 & \text{for } \text{RELSDI} > 0.85 \end{array}$$

where RELSDI = current stand density index / maximum stand density index

## **4.3 BARK RATIO RELATIONSHIPS**

Bark ratio estimates are used to convert between diameter outside bark and diameter inside bark in various parts of the model. Equation forms used in the Central Rockies variant are shown below, and coefficients for these equations are shown in Table 8.

Equation forms:

$$\{1\} \text{ BRATIO} = b_1 + b_2 * [1/\text{DBH}]$$

$$\{2\} \text{ BRATIO} = b_1$$

BRATIO = bark ratio (bounded to be  $0.80 \leq \text{BRATIO} \leq 0.99$ )

DBH = tree diameter at breast height (bounded to be  $\text{DBH} \geq 1.0$  for this calculation)

Table 8. Coefficients for the bark ratio equations in the Central Rockies FVS variant.

FVS Number = Alpha Code; Model Type	Equation Form	b <sub>1</sub>	b <sub>2</sub>	Equation Source
1 = AF	2	0.890	0.	PP from Wykoff, et. al. 1982
2 = CB	2	0.890	0.	PP from Wykoff, et. al. 1982
3 = DF	2	0.867	0.	Wykoff, et. al. 1982
4 = GF	2	0.890	0.	PP from Wykoff, et. al. 1982
5 = WF	2	0.890	0.	PP from Wykoff, et. al. 1982
6 = MH	2	0.9497	0.	Wykoff, et. al. 1982
7 = RC	2	0.9497	0.	Wykoff, et. al. 1982
8 = WL	1	0.87407	-0.185	Schmidt, et. al. 1976
9 = BC	1	0.9625	-0.1141	Uses LP equation
10 = LM	1	0.9625	-0.1141	Uses LP equation
11 = LP	1	0.9625	-0.1141	Myers 1964
12 = PI; SM, SP	1	0.8967	-0.4448	PP from Dolph PSW-368
12 = PI; all other	1*	0.9002	-0.3089	Uses PP equation
13 = PP; SM, SP	1	0.8967	-0.4448	PP from Dolph PSW-368
13 = PP; all other	1*	0.9002	-0.3089	Myers & Van Deusen 1958
14 = WB	1	0.9625	-0.1141	Uses LP equation
15 = WP	2	0.9643	0.	Wykoff, et. al. 1982
16 = JU; SM, SP	1	0.8967	-0.4448	PP from Dolph PSW-368
16 = JU; all other	1*	0.9002	-0.3089	Uses PP equation
17 = BS	1	0.9502	-0.2528	Uses ES equation
18 = ES	1	0.9502	-0.2528	Myers & Alexander 1972
19 = WS	1	0.9502	-0.2528	Uses ES equation
20 = AS	2	0.950	0.	Utah FVS variant
21 = CO	1	0.892	-0.086	Edminster, et. al. 1977
22 = OA	1	0.93789	-0.24096	Clark, et. al. 1991
23 = OS; SM, SP	1	0.8967	-0.4448	PP from Dolph PSW-368
23 = OS; all other	1*	0.9002	-0.3089	Uses PP equation
24 = OH	1	0.892	-0.086	Uses CO equation

\* DBH limited to  $1.0 \leq \text{DBH} \leq 19.0$  inches in this calculation

#### **4.4 CROWN COMPETITION FACTOR AND CROWN WIDTH**

The Central Rockies variant uses crown competition factor (CCF) as a predictor variable in some growth relationships, and crown width for each tree is reported on the tree list output table and used for percent cover calculations in the model. Crown competition factor for an individual tree is calculated using equation {5}, the coefficients shown in Table 9, and the appropriate equation index from Table 10. Crown competition factor, on a per-acre basis, is computed by multiplying the individual tree CCF values by the tree's per-acre representation, and summing these products over all trees in the stand. Crown width is calculated using equation {6}.

$$\begin{array}{ll}
 \{5\} \text{ CCFT} = 0.001 & \text{for } \text{DBH} \leq 0.1 \\
 \text{CCFT} = a * \text{DBH}^b & \text{for } 0.1 < \text{DBH} < 10.0 \\
 \text{CCFT} = c + d * \text{DBH} + e * \text{DBH}^2 & \text{for } \text{DBH} \geq 10.0
 \end{array}$$

where CCFT = crown competition factor for an individual tree  
 DBH = diameter at breast height  
 and coefficients are shown in Table 9

{6} Crown Width = square root [CCFT / 0.001803]

Table 9. Coefficients for the crown competition factor equations used in the Central Rockies Variant

Equation Index	a	b	c	d	e
1	0.009187	1.76	0.01925	0.0167	0.00365
2	0.017299	1.5571	0.11	0.0333	0.00259
3	0.015248	1.7333	0.04	0.0270	0.00405
4	0.011109	1.7250	0.03	0.0215	0.00363
5	0.008915	1.78	0.03	0.0238	0.00490
6	0.007875	1.7360	0.03	0.0173	0.00259
7	0.011402	1.7560	0.03	0.0216	0.00405
8	0.007813	1.7680	0.03	0.0180	0.00281

Table 10. Index to crown competition factor equations used in the Central Rockies Variant

FVS Number = Alpha Code	SM model type Equation Index	SP model type Equation Index	BH model type Equation Index	SF model type Equation Index	LP model type Equation Index
1 = AF	7	3	1	7	7
2 = CB	7	3	1	7	7
3 = DF	2	2	2	2	2
4 = GF	7	3	1	7	7
5 = WF	3	3	1	7	7
6 = MH	1	1	1	1	1
7 = RC	1	1	1	1	1
8 = WL	1	1	1	1	1
9 = BC	1	1	1	1	1
10 = LM	1	1	1	1	1
11 = LP	1	1	1	1	1
12 = PI	1	7	1	1	1
13 = PP	8	8	8	1	8
14 = WB	1	1	1	1	1
15 = WP	1	1	1	1	1
16 = JU	1	1	1	1	1
17 = BS	1	1	6	6	6
18 = ES	6	1	6	6	6
19 = WS	6	1	6	6	6
20 = AS	5	5	5	5	5
21 = CO	4	4	1	4	4
22 = OA	4	6	4	4	4
23 = OS	1	1	1	1	1
24 = OH	4	4	4	4	4

#### **4.5 SMALL TREE GROWTH RELATIONSHIPS**

Trees are considered “small” trees for FVS modeling purposes when they are smaller than some threshold diameter. This threshold diameter is a function of the lower diameter limit in the data used to fit the model, and how well the model formulation used to estimate growth on “large” trees fits trees in the lower end of the diameter range. In the Central Rockies variant, the threshold diameter for each species is shown in Table 11.

Table 11. Threshold diameters for switching between small tree growth equations and large tree growth equations in the Central Rockies FVS variant, and the range of diameters (minimum and maximum) over which small tree height growth estimates are weighted with large tree estimates to assure a smooth transition between the two model formulations.

FVS Number	Alpha Code	Common Name	Threshold dbh	Minimum DBH	Maximum DBH
1	AF	Subalpine fir	1.0	0.5	2.0
2	CB	Corkbark fir	1.0	0.5	2.0
3	DF	Douglas-fir	1.0	0.5	2.0
4	GF	Grand fir	3.0	2.0	5.0
5	WF	White fir	1.0	0.5	2.0
6	MH	Mountain hemlock	3.0	2.0	4.0
7	RC	Western redcedar	3.0	2.0	5.0
8	WL	Western larch	3.0	2.0	5.0
9	BC	Bristlecone pine	99.0*	99.0*	N/a
10	LM	Limber pine	2.0	0.5	4.0
11	LP	Lodgepole pine	1.0	0.5	2.0
12	PI	Pinyon pine	99.0*	99.0*	N/a
13	PP	Ponderosa pine	1.0	0.5	2.0
14	WB	Whitebark pine	1.0	0.5	2.0
15	WP	Western white pine	1.0	0.5	2.0
16	JU	Western juniper	99.0*	99.0*	N/a
17	BS	Blue spruce	1.0	0.5	2.0
18	ES	Engelmann spruce	1.0	0.5	2.0
19	WS	White spruce	1.0	0.5	2.0
20	AS	Quaking aspen	1.0	0.5	2.0
21	CO	Cottonwoods	1.0	0.5	2.0
22	OA	Oaks	99.0*	99.0*	N/a
23	OS	Other softwoods	1.0	0.5	2.0
24	OH	Other hardwoods	1.0	0.5	2.0

\*There is only one growth relationship that applies to trees of all sizes for these species. These relationships are contained in the “small” tree portion of FVS.

The small tree model is height-growth driven. That is to say, height growth is estimated first, then diameter growth is estimated from height growth, and finally crown ratio change is estimated. These components are discussed in the following sections.

#### 4.5.1 Small Tree Height Growth

Data was not available to fit small tree height growth models for the Central Rockies variant for species other than aspen. As a result, for all species except aspen, the CR variant uses a blend of theoretical models for CR, and small tree height growth modifier equations from the Utah FVS variant. Potential height growth is estimated as a function of site index, and then is modified to account for density effects and tree vigor.

Potential height growth is estimated as follows:

$$\{7\} \text{ RELSI} = (\text{SI} - \text{SITELO}) / (\text{SITEHI} - \text{SITELO})$$

$$\{8\} \text{ POTHTG} = \text{SI} / [(15.0 - 4.0 * \text{RELSI}) * C]$$

where RELSI = relative site index

SI = site index

SITELO = lower end of the site range for this species (see Table 12)

SITEHI = upper end of the site range for this species (see Table 12)

POTHTG = potential height growth

C = constant (1.10 for red cedar and western larch; 1.0 for all other species)

If the site index for the stand is less than or equal to the lower site limit, it is set to the lower limit + 0.5 for the calculation of RELSI. Similarly, if the site index for the stand is greater than the upper site limit, it is set to the upper site limit for the calculation of RELSI.

Table 12. Site index range used for the calculating small tree height growth in the Central Rockies FVS variant

FVS Number	Alpha Code	Common Name	SITELO	SITEHI
1	AF	Subalpine fir	40	105
2	CB	Corkbark fir	30	100
3	DF	Douglas-fir	40	120
4	GF	Grand fir	30	130
5	WF	White fir	40	105
6	MH	Mountain hemlock	40	70
7	RC	Western redcedar	20	125
8	WL	Western larch	40	120
9	BC	Bristlecone pine	20	60
10	LM	Limber pine	10	60
11	LP	Lodgepole pine	30	95
12	PI	Pinyon pine	6	40
13	PP	Ponderosa pine	30	100
14	WB	Whitebark pine	20	60
15	WP	Western white pine	30	130
16	JU	Western juniper	6	30
17	BS	Blue spruce	30	110
18	ES	Engelmann spruce	40	120
19	WS	White spruce	30	85
20	AS	Quaking aspen	20	100
21	CO	Cottonwoods	30	120
22	OA	Oaks	6	40
23	OS	Other softwoods	30	95
24	OH	Other hardwoods	20	100

Once potential height growth is estimated, the height growth modifiers are calculated. The density related modifier is based on stand crown competition factor and average height of the 40 largest diameter trees, equation {9}.

$$\{9\} \text{ PCTRED} = 1.11436 - 0.011493 * X + 0.43012E-04 * X^2 - 0.72221E-07 * X^3 + 0.5607E-10 * X^4 - 0.1641E-13 * X^5$$

where X = AVHT \* (CCF/100.) with an upper bound of X=300.

and PCTRED = reduction proportion in height growth due to stand density

AVHT = average height of the 40 largest diameter trees in the stand

CCF = stand crown competition factor

PCTRED is bounded on the upper side at 1.0, and on the lower side at 0.01. The vigor multiplier is based on a trees live crown ratio, equation {10}.

$$\{10\} \text{ VIGOR} = (150 * \text{CR}^3 * e^{(-6 * \text{CR})}) + 0.3$$

where VIGOR = reduction proportion in height growth due to tree vigor  
 CR = a trees' live crown ratio (compacted) expressed as a proportion

VIGOR is bounded on the upper side at 1. The vigor modifier is reduced, equation {11}, for pinyon pine, juniper, oaks, and bristlecone pine.

$$\{11\} \text{ VIGOR} = 1 - [(1 - \text{VIGOR}) / 3] \quad \text{for pinyon, juniper, oaks, and bristlecone pine}$$

Small tree height growth for an individual tree other than aspen is then estimated as the potential height growth adjusted by these two modifiers, equation {12}. A small random error is added to this estimate, and the estimate is then adjusted to account for cycle length and any user defined small-tree height growth adjustments.

$$\{12\} \text{ Height growth} = \text{POTHTG} * \text{PCTRED} * \text{VIGOR}$$

Height growth for small aspen is obtained from a height-age curve (Shepperd 1995). Shepperd's original curve seemed to overestimate height growth and is reduced by 25 percent in this variant, equation {13}.

$$\{13\} \text{ Height} = (26.9825 * \text{Age}^{1.1752}) * 0.75$$

where Height is total tree height in centimeters and Age is the total tree age

A height is estimated from the trees' current age, and then it's current age plus 10 years. Height growth is the difference between these two height estimates adjusted to account for cycle length and any user defined small-tree height growth adjustments for aspen, and converted from centimeters to feet. An estimate of the tree's current age is obtained at the start of a projection using the tree's height and solving equation {13} for age.

Height growth estimates from the small tree model are weighted, using equation {14}, with height growth estimates from the large tree model to assure a smooth transition between the two models.

$$\{14\} \text{ Predicted height growth} = (\text{small tree height growth}) * (1 - \text{weight}) + (\text{large tree height growth}) * \text{weight}$$

where weight = (diameter – minimum DBH) / (maximum DBH – minimum DBH)  
 weight = 0 if diameter is less than the minimum DBH shown in Table 11  
 weight = 1 if diameter is greater than the maximum DBH shown in Table 11

## 4.5.2 Small Tree Diameter Growth

The height-diameter functions discussed in the Height – Diameter Relationships section are used to estimate small tree diameter growth for all species except ponderosa pine, bristlecone pine, pinyon pine, juniper, and oaks. The functions are algebraically solved to estimate diameter as a function of height. Height at the start of the projection cycle is known, and height at the end of the cycle is obtained by adding the height growth (as described in section 4.5.1) to the starting height. A predicted diameter at the start of the projection cycle is estimated from the height at the start of the projection cycle, and a predicted diameter at the end of the projection cycle is estimated from the height at the end of the projection cycle. Small tree diameter growth is calculated as the difference between predicted diameter at the start of the projection period and the predicted diameter at the end of the projection period, adjusted for bark ratio.

Ponderosa pine uses equation {14a} in the same manner as just described for the other species.

$$\{14a\} \text{ Diameter at breast height} = (\text{height} - 4.17085) / 3.03659$$

Bristlecone pine, pinyon pine, juniper, and oaks use equation {14b} as previously described.

$$\{14b\} \text{ Diameter at breast height} = (\text{height} - 4.5) * 10 / (\text{SI} - 4.5)$$

where SI is the site index for the individual species

### 4.5.3 Crown Ratio Change

See section 4.6.3 in the Large Tree Growth Relationships section 4.6.

## 4.6 LARGE TREE GROWTH RELATIONSHIPS

The large tree model in FVS is diameter-growth driven. That is to say, diameter growth is estimated first, then height growth is estimated from diameter growth and other variables, and finally crown ratio change is estimated. Most of the large tree diameter equations are from Edminster's GENGYM growth and yield model. However, equations from other variants are used for certain species not represented very well in the data used to develop GENGYM, or in cases where the GENGYM equations did not perform satisfactorily. Species not represented well in the data, are generally found at the extreme northern range of the Central Rockies variant. These are a relatively minor component of the area covered by this variant. In GENGYM, a single equation was used to estimate the diameter growth for bristlecone pine, pinyon pine, western juniper and oaks. This equation did not perform satisfactorily for these species and is not used for these species in this variant. However, this equation is used in both GENGYM and this variant for estimating diameter growth on trees classified as "other softwoods".

### 4.6.1 Large Tree Diameter Growth

Of the 24 species in this variant, 14 use the GENGYM diameter growth equations. Equations from GENGYM predict a tree's future diameter based on stand and tree variables. The equation form is shown in {15} with coefficients shown in Table 13.

$$\{15\} \text{ DF} = a_0 + a_1 * \text{DBH} + a_2 * \text{BA} + a_3 * \text{SI} + a_4 * [\text{LN}(\text{DBH})]^2 + a_5 * \text{BGT TBA} + a_6 * \text{LN}(\text{BATEM}) + a_7 * \text{DBH}^2$$

where  
 DF = end of cycle diameter at breast height  
 DBH = current tree diameter at breast height (DBH  $\geq$  1.0 for this computation)  
 BA = total stand basal area  
 SI = site index  
 BGT TBA = basal area above this tree's diameter class / total stand basal area  
 BATEM = total stand basal area  
 LN = natural logarithm

BGT TBA and BATEM are subject to the following restrictions:  
 Southwestern Mixed Conifers model type:  
 BATEM  $\geq$  1.0  
 If BATEM is less than 65, then BGT TBA is set to 0.  
 Southwestern Ponderosa Pine model type:

BATEM  $\geq$  21.  
 Black Hills Ponderosa Pine and Spruce-Fir model types:  
 BATEM  $\geq$  5.  
 Lodgepole pine model type:  
 BATEM  $\geq$  14.

Table 13. Coefficients for calculating large tree diameter growth in the Central Rockies FVS variant, for species using the GENGYM equations.

FVS Number = Alpha Code: Model Type	a <sub>0</sub>	DBH a <sub>1</sub>	BA a <sub>2</sub>	SI a <sub>3</sub>	LN( DBH) <sup>2</sup> a <sub>4</sub>	BGTTBA a <sub>5</sub>	LN( BATEM) a <sub>6</sub>	DBH <sup>2</sup> a <sub>7</sub>
1 = AF: SM,SP	0.50283	0.93999	-0.0016822	0.00791	0.16235			
1 = AF: all other	2.19459	0.94659		0.00615	0.11326	-0.20410	-0.35970	
2 = CB: SM,SP	0.50283	0.93999	-0.0016822	0.00791	0.16235			
2 = CB: all other	2.19459	0.94659		0.00615	0.11326	-0.20410	-0.35970	
3 = DF: all	0.58234	0.94542	-0.0025092	0.00705	0.15738	-0.14044		
4 = GF: **								
5 = WF: all	0.46172	1.04089	-0.0019984	0.00659		-0.09197		-0.0011355
6 = MH: **								
7 = RC: **								
8 = WL: **								
9 = BC: ***								
10 = LM: **								
11 = LP: all	1.32652	0.96279		0.00590	0.06298	-0.17138	-0.21827	
12 = PI: ***								
13 = PP: SM*	0.26265	0.94001	-0.0016405	0.00601	0.16328			
13 = PP: SP	4.10552	0.88872		0.01378	0.23834	-0.52784	-0.83531	
13 = PP: BH*	2.50428	0.94573		0.01354	0.05940	-0.46350	-0.45765	
13 = PP: LP,SF	2.50428	0.94573		0.01354	0.05940	-0.46350	-0.45765	
14 = WB: **								
15 = WP: all	0.89451	0.95435	-0.0012183	0.00159	0.09987	-0.20815		
16 = JU: ***								
17 = BS: all	0.50941	1.02697	-0.0035783	0.01022				-0.0009882
18 = ES: SM,SP	0.67074	1.03068	-0.0020055	0.00633				-0.0010875
18 = ES: all other	2.28652	0.94475		0.01295	0.10778	-0.48056	-0.41632	
19 = WS: all	2.94734	0.88423		0.01207	0.25363		-0.64449	
20 = AS: SM,SP	0.24506	1.01291	-0.0008466	0.00631				
20 = AS: all other	1.55986	1.01825		0.00672		-0.00073	-0.29342	
21 = CO: SM,SP	0.24506	1.01291	-0.0008466	0.00631				
21 = CO: all other	1.55986	1.01825		0.00672		-0.00073	-0.29342	
22 = OA: ***								
23 = OS: all	0.25897	1.03129	-0.0002025	0.00177				
24 = OH: SM,SP	0.24506	1.01291	-0.0008466	0.00631				
24 = OH: all other	1.55986	1.01825		0.00672		-0.00073	-0.29342	

Coefficients shown as blanks are equal to zero.

\*see discussion below

\*\*uses equations from another variant; described below

\*\*\*uses the equations described for the small tree model for all sized trees

In the Southwestern Mixed Conifer (SM) model type, the estimated future diameter for ponderosa pine is a blend {16} of the estimate using the equation shown for the SM model type and an estimate from the equation shown for the Southwestern Ponderosa Pine (SP) model type.

$$\{16\} DF = (1.0 - \text{FACTOR}) * \text{SMDF} + \text{FACTOR} * \text{SPDF}$$

where DF = end of cycle diameter (blended)  
 FACTOR = adjustment factor which is the maximum of ADJB and ADJR, shown below  
 SMDF = estimated future diameter using the SM model type equation  
 SPDF = estimated future diameter using the SP model type equation

and

$$\begin{aligned} \text{ADJB} &= 0.0 && \text{for stand basal area} \geq 100 \\ &= 2.5 - 0.025 * \text{stand basal area} && \text{for } 60 < \text{stand basal area} < 100 \\ &= 1.0 && \text{for stand basal area} \leq 60 \end{aligned}$$

$$\begin{aligned} \text{ppratio} &= \text{ponderosa pine basal area} / \text{stand basal area} \\ \text{ADJR} &= 0.0 && \text{for } \text{ppratio} \leq 0.3 \\ &= -1.5 + 5.0 * \text{ppratio} && \text{for } 0.3 < \text{ppratio} < 0.5 \\ &= 1.0 && \text{for } 0.5 \leq \text{ppratio} \end{aligned}$$

Similarly, in the Black Hills Ponderosa pine (BH) model type, the estimated future diameter for ponderosa pine is a blend if certain conditions are met, and a direct estimate otherwise. Those conditions are: (1) whether the stand is considered uneven-aged; (2) whether the tree exists in an overtopped condition; and (3) whether the estimated future diameter using the BH equation is greater than the estimated future diameter using the SP equation. A stand is considered uneven-aged if the range in age between the 5<sup>th</sup> percentile tree and the 95<sup>th</sup> percentile tree exceeds 40 years. A tree is considered overtopped if at least 30 percent of the stand basal area is in diameter classes larger than this trees' diameter class (1 inch classes). If all three of these conditions are met, the estimated future diameter is a blend {17} of the estimate using the equation shown for the BH model type and an estimate from the equation shown for the Southwestern Ponderosa Pine (SP) model type.

$$\begin{aligned} \{17\} DF &= \text{SPDF} && \text{for } \text{baratio} \geq 0.5 \\ DF &= (2.5 - 5.0 * \text{baratio}) * \text{BHDF} + (-1.5 + 5.0 * \text{baratio}) * \text{SPDF} && \text{for } 0.3 < \text{baratio} < 0.5 \end{aligned}$$

where DF = estimated future diameter (blended)  
 SPDF = estimated future diameter using the SP model type equation  
 BHDF = estimated future diameter using the BH model type equation  
 baratio = basal area in dbh classes larger than this trees dbh class / total stand basal area

Since the FVS large tree model logic is based on the natural logarithm of change in diameter squared (DDS), estimated future diameter is converted to this basis by first calculating diameter growth (inside bark) using equation {18}, adjusting this value to account for a stagnation effect {19}, and then converting the result to a DDS basis using equation {20}.

$$\{18\} \text{DIAGR} = (\text{Estimated Future Diameter} - \text{Current Diameter}) * \text{Bark Ratio}$$

$$\begin{aligned} \{19\} \text{DIAGR} &= \text{DIAGR} * \text{Stagnation Multiplier} && \text{for species other than Black Hills ponderosa pine} \\ &= \text{DIAGR} * \text{Stagnation Multiplier} * 0.8 && \text{for ponderosa pine in the Black Hills model type} \end{aligned}$$

$$\{20\} \text{DDS} = \text{LN} [ (\text{DIAGR} * \{ (2.0 * \text{Current Diameter} * \text{Bark Ratio}) + \text{DIAGR} \}) ]$$

Six species use large tree diameter growth relationships from other variants, which predict DDS directly. The grand fir equation is from the Central Idaho variant. Equations for mountain hemlock, western red cedar, and western larch are from the North Idaho variant for elevation set at 6000 feet and habitat types set to 710 (TSME/XETE), 550

(THPL/OPHO), and 260 (PSME/PHMA) respectively. The limber pine equation is from the Utah variant. The whitebark pine equation is from the Eastern Montana variant for elevation set at 8000 feet and habitat type set to 850 (PIAL-ABLA). The equation form for all these species is shown in {21} with species-specific coefficients shown in Table 14.

$$\begin{aligned} \{21\} \text{ DDS} = & a_0 + a_1 * \text{SIN}(\text{ASPECT}) * \text{SLOPE} + a_2 * \text{COS}(\text{ASPECT}) * \text{SLOPE} + a_3 * \text{SLOPE} \\ & + a_4 * \text{SLOPE}^2 + a_5 * \text{LN}(\text{DBH}) + a_6 * \text{DBH}^2 \\ & + a_7 * \text{BAL} + a_8 * \text{CR} + a_9 * \text{CR}^2 + a_{10} * \text{LN}(\text{BA}) + a_{11} * \text{PCCF} \\ & + a_{12} * \text{BAL}/\text{LN}(\text{DBH}+1) + a_{13} * \text{PBAL}/\text{LN}(\text{DBH}+1) \\ & + a_{14} * \text{LN}(\text{RELDEN}) + a_{15} * \text{RELDEN} + a_{16} * \text{SI} \end{aligned}$$

- where: SIN = trigonometric sine function  
 COS = trigonometric cosine function  
 LN = natural logarithm  
 ASPECT = stand aspect  
 SLOPE = stand slope in percent  
 DBH = tree diameter at breast height  
 BAL = total stand basal area in trees larger than this tree  
 CR = crown ratio expressed as a proportion  
 BA = total stand basal area  
 PCCF = crown competition factor for the sampling point where the tree is located  
 RELDEN = crown competition factor for the stand  
 PBAL = basal area on the sampling point in trees larger than this tree  
 SI = site index

Table 14. Coefficients for calculating large tree diameter growth in the Central Rockies FVS variant, for species using DDS equations from other variants

Coefficient	Grand Fir	Mtn hemlock	W Red Cedar	W Larch	Limber Pine	Whitebark Pine
a <sub>0</sub>	0.88728	0.19489	1.26832	1.39215	1.911884	-0.5933
a <sub>1</sub>	0.009335	0.13363	0.05534	0.03430	-0.01752	-0.01606
a <sub>2</sub>	-0.004469	0.17935	-0.06625	-0.21337	-0.609774	0.00270
a <sub>3</sub>	-0.033374	0.07628	0.11931	0.33523	-2.05706	-0.20011
a <sub>4</sub>	-0.418343			-0.70216	2.113263	
a <sub>5</sub>	1.286963	0.89778	0.58705	0.54140	0.213947	0.80110
a <sub>6</sub>	-0.0004408	-0.000484		-0.000310	-0.0006538	
a <sub>7</sub>			0.0074596	0.0043637	-0.00358634	0.00064
a <sub>8</sub>	1.175105	1.28403	1.29360	1.03478	1.523464	1.02878
a <sub>9</sub>	0.219013			0.07509		-0.45448
a <sub>10</sub>	-0.217923					
a <sub>11</sub>	-0.000512					
a <sub>12</sub>		-0.006611	-0.0228375	-0.0203256		-0.00328
a <sub>13</sub>	-0.000578					
a <sub>14</sub>						-0.25717
a <sub>15</sub>		-0.0010744	-0.0015356	-0.0005438	-0.00199592	
a <sub>16</sub>					0.001766	

\*Coefficients shown as blanks are equal to zero.

Once DDS is estimated using equation {21}, it must be transformed into a real scale diameter growth using equation {22}, adjusted for the stagnation effect {23}, and then converted back to DDS scale {20} for further processing.

$$\{22\} \text{ DIAGR} = \text{SQRT} \{ \text{EXP}(\text{DDS}) + [(\text{DBH} * \text{Bark Ratio})^2] \} - \text{DBH} * \text{Bark Ratio}$$

$$\{23\} \text{ DIAGR} = \text{DIAGR} * \text{Stagnation Multiplier}$$

For bristlecone pine, pinyon pine, juniper, and oaks, the equations described in the small tree model section are used for trees of all sizes.

## 4.6.2 Large Tree Height Growth

Height growth equations used in the Central Rockies variant for large trees have the same origins as the diameter growth equations used for large trees. In other words, equations for 14 of the species come from the GENGYM model, equations for 6 species come from other variants, and 4 species use the equations described in the small tree model section.

The equations from GENGYM predict height growth from the site index curves listed in Table 4 for even-aged stands, and height growth from a regression equation for uneven-aged stands. These estimates get blended when certain conditions are met.

### 4.6.2.1 EVEN-AGED STANDS HEIGHT GROWTH ESTIMATE

First a height is estimated from the site curve using the beginning of cycle DBH and estimated tree age. Next, a second height is estimated from the site curves using the end of cycle DBH and the estimated age plus 10 years. The 10-year even-aged height growth estimate is then the difference between these two estimates.

#### 4.6.2.1.1 SW Mixed Conifers Model Type

The even-aged height growth estimation sequence is a four-step process. First an age is determined, second heights from the guide curve and the lower 95 percent confidence interval are estimated, third these estimates are combined, and fourth a reduction is made for a tree's position in the canopy. A detailed description of formula derivation is contained in Edminster, Mathiasen, and Olsen (1991).

The first step is determining an age (AGETEM) to use in the calculation. AGETEM is first set to the tree's age, or 210 years, whichever is less. If the site index is less than 80 and the value of (110 – Site Index) is greater than the value of AGETEM as just determined, then AGETEM is set to the value (110 – Site Index).

Second, total tree height on the appropriate guide curve (HG) is determined using equation {24}.

$$\{24\} \text{ HG} = 4.5 + 109.559129 * (1 - 0.975884 * e^{-0.014377 * \text{AGETEM}})^{1.289266}$$

The estimated height of the lower bound of the 95 percent confidence interval (HL) is determined using equation {25}.

$$\{25\} \text{ HL} = 72.512644 * (1 - 0.876961 * e^{-0.020066 * \text{AGETEM}})^{2.016632}$$

Third, the estimates are combined using equation {26}.

$$\{26\} \text{ HT} = -[(\text{HG} - \text{HL}) * ((82.488 - \text{Site Index}) / 26.279)] + \text{HG}$$

where HT = the even-aged height estimate, given the tree's age

If site index is 80, or greater, and the tree's age is less than AGETEM as determined above, HT is further modified using equation {27}.

$$\{27\} HT = 4.5 + [(HT - 4.5) / AGETEM] * \text{tree age}$$

If site index is greater than or equal to 80 and AGETEM is less than 20, then the estimate of HT, using equations {26} and {27}, is replaced by an estimate of HT using equation {28}.

$$\{28\} HT = 4.5 + [(0.02348 * \text{Site Index}) - 0.93429] * AGETEM$$

And finally, the estimated HT is multiplied by an adjustment factor {29} to account for a tree's position in the canopy.

$$\{29\} HT = HT * \text{FACTOR}$$

where FACTOR = (1 - basal area above the trees' diameter class / total stand basal area)  
and FACTOR is constrained to be in the interval (0.768 - 1.0)

#### 4.6.2.1.2 SW Ponderosa Pine Model Type

The even-aged height growth estimation sequence is similar to that for the SM model type. First an age is determined to use in the calculation, second heights from the guide curve and the lower 95 percent confidence interval are estimated, third these estimates are combined, and fourth a reduction is made for a trees position in the canopy. A detailed description of formula derivation is contained in Minor (1964).

The first step is determining an age (AGETEM) to use in the calculation. AGETEM is first set to the tree's age, or 210 years, whichever is less. If the site index is less than 80 and the value of (120 - Site Index) is greater than the value of AGETEM as just determined, then AGETEM is set to (120 - Site Index).

Second, total tree height on the appropriate guide curve (HG) is determined using equation {30}.

$$\{30\} HG = 4.5 + 106.493954 * (1 - 0.938775 * e^{-0.016066 * AGETEM})^{1.550720}$$

The estimated height of the lower bound of the 95 percent confidence interval (HL) is determined using equation {31}.

$$\{31\} HL = 78.078735 * (1 - 0.843715 * e^{-0.020412 * AGETEM})^{2.280435}$$

Third, the estimates are combined using equation {32}.

$$\{32\} HT = -[(HG - HL) * ((81.5585 - \text{Site Index}) / 21.7149)] + HG$$

where HT = even-aged height estimate given the tree's age

If site index is 80, or greater, and the tree's age is less than AGETEM as determined above, HT is further modified using equation {27}.

If site index is greater than or equal to 80 and AGETEM is less than 20, then the estimate of HT using equations {32} and {27} is replaced by an estimate of HT using equation {33}.

$$\{33\} HT = 4.5 + [(0.02463 * \text{Site Index}) - 1.1025] * AGETEM$$

And finally, the estimate HT is multiplied by an adjustment factor {29} to account for a trees position in the canopy.

#### 4.6.2.1.3 Black Hills Ponderosa Pine Model Type

Even-aged height is estimated using Meyer's (1961) ponderosa pine site curves. If the trees' height is above the height at which the site curve flattens off {34}, or the tree is over 165 years old, 10-year height growth is set to 0.1 foot.

$$\{34\} \text{ Height at which site curve flattens off} = (\text{Site Index} + 0.3846) * 1.2999886$$

Otherwise, height is calculated using equation {35}.

$$\{35\} \text{ HT} = (\text{Site Index} + 0.3846) * (-0.5234 + 1.8234 * e^{-(1.0989 - 0.006105 * \text{tree age}) 2.35})$$

A height is estimated for the tree's current age and the current age + 10 years. Height growth is then the difference between these two estimates {36}, and is modified using equation {37}.

$$\{36\} \text{ HTG} = \text{HT}_{10} - \text{HT}_{\text{NOW}}$$

where HTNOW is equation {35} evaluated with the current tree age  
 HT10 is equation {35} evaluated with the current tree age + 10 years

$$\{37\} \text{ HTG} = \text{HTG} * \text{FACTOR}$$

where FACTOR = (1 – basal area above the trees' diameter class / total stand basal area)  
 and FACTOR is constrained to be in the interval (0.793 – 1.0)

So the estimate in the Black Hills model type is actually a height growth estimate, rather than a height estimate. This is a minor, but necessary, point relating to the discussion below on combining estimates.

#### 4.6.2.1.4 Spruce-fir Model Type

Even-aged height is estimated using Alexander's (1967) site curves for Engelmann spruce and sub-alpine fir. Height is estimated using equation {38} with AGETEM being the tree age or 30, whichever value is greater.

$$\{38\} \text{ HT} = 4.5 + (2.75780 * \text{Site Index}^{0.83312}) * [1 - e^{(-0.015701 * \text{tree age})}]^{(22.71944 * \text{Site Index}^{-0.63557})}$$

If the tree age is less than 30 years, then the height estimate is modified using equation {39}.

$$\{39\} \text{ HT} = 4.5 + [(\text{HT} - 4.5) / \text{AGETEM}] * \text{tree age}$$

And finally, the height estimate is modified for the trees' crown position using equation {40}.

$$\{40\} \text{ HT} = \text{HT} * \text{FACTOR}$$

where FACTOR = (1 – basal area above the trees' diameter class / total stand basal area)  
 and FACTOR is constrained to be in the interval (0.728 – 1.0)

#### 4.5.2.1.5 Lodgepole Pine Model Type

Even-aged height is estimated using Alexander, Tackle, and Dahms (1967) lodgepole pine site index curves. Height is estimated using equation {41} with AGETEM being the tree age constrained to the interval (30 – 200 years).

$$\{41\} \text{ HT} = 9.89331 - 0.19177 * \text{AGETEM} + 0.00124 * \text{AGETEM}^2 - 0.00082 * \text{CCFTEM} * \text{SI} + 0.01387 * \text{AGETEM} * \text{SI} - 0.0000455 * \text{AGETEM}^2 * \text{SI}$$

where SI = Site Index

CCFTEM = (stand crown competition factor – 125) constrained to be  $\geq 0$

If the tree age is less than 30 years, the estimate of HT is further modified using equation {42}.

$$\{42\} HT = (HT / AGETEM) * \text{tree age}$$

And finally, the height estimate is modified using equation {43} to account for the trees' crown position.

$$\{43\} HT = HT * FACTOR$$

where FACTOR = (1 – basal area above the trees' diameter class / total stand basal area)  
and FACTOR is constrained to be in the interval (0.742 – 1.0)

#### 4.6.2.2 UNEVEN-AGED STANDS HEIGHT GROWTH ESTIMATE

Equations from GENGYM predict a tree's future height based on stand and tree variables. The equation form is shown in {44} with coefficients shown in Table 15.

$$\{44\} HTU = 4.5 + a_1 * SI^{a_2} * [1 - \exp(a_3 * DBH)]^{(a_4 * BATEM)^{a_5}}$$

for AF & CB in model types 1, 2;  
DF; WF; OS; PP; WP; BS; WS;  
ES in model types 1,2;  
AS, CO & OH in model types 1,2

$$HTU = 4.5 + (a_1 + a_2 * SI) * [1 - \exp(a_3 * DBH)]^{(a_4 * BATEM)^{a_5}}$$

for AF & CB in model types 3, 4, 5;  
LP; WB;  
ES in model types 3,4,5;  
AS, CO & OH in model types 3,4,5

where HTU = end of cycle total height uneven-aged estimate  
DBH = current tree diameter at breast height  
SI = site index  
BATEM = total stand basal area  
and  $a_1 - a_5$  are coefficients shown in Table 15

BATEM is subject to the following restrictions:  
Southwestern Mixed Conifers model type:  
BATEM  $\geq 1.0$   
Southwestern Ponderosa Pine model type:  
BATEM  $\geq 21$ .  
Black Hills Ponderosa Pine and Spruce-Fir model types:  
BATEM  $\geq 5$ .  
Lodgepole pine model type:  
BATEM  $\geq 14$ .

Table 15. Coefficients for calculating large tree height uneven-aged estimate in the Central Rockies FVS variant, for species using the GENGYM equations.

FVS Number = Alpha Code: Model Type	a <sub>1</sub>	a <sub>2</sub>	a <sub>3</sub>	a <sub>4</sub>	a <sub>5</sub>
1 = AF: SM,SP	4.514294	0.755380	-0.080869	1.409884	0.003919
1 = AF: all other	15.5	1.1	-0.097152	4.698567	-0.252630
2 = CB: SM,SP	4.514294	0.755380	-0.080869	1.409884	0.003919
2 = CB: all other	15.5	1.1	-0.097152	4.698567	-0.252630
3 = DF: all	13.096420	0.480509	-0.077408	1.237589	-0.063297
4 = GF: **					
5 = WF: all	13.822088	0.462393	-0.075766	1.312638	-0.040708
6 = MH: **					
7 = RC: **					
8 = WL: **					
9 = BC: ***					
10 = LM: **					
11 = LP: all	8.5	1.1	-0.085004	1.709643	-0.163186
12 = PI: ***					
13 = PP: SM	24.244690	0.343864	-0.069180	1.251384	-0.272018
13 = PP: SP	40.78321	0.332614	-0.021471	0.922811	-0.133923
13 = PP: BH,LP,SF	32.108633	0.276926	-0.057766	0.984340	-0.169876
14 = WB: all	8.5	1.1	-0.085004	1.709643	-0.163186
15 = WP: all	18.967185	0.379790	-0.071482	1.159608	-0.099449
16 = JU: ***					
17 = BS: all	54.180173	0.177962	-0.089253	1.533535	-0.028852
18 = ES: SM,SP	10.616238	0.549461	-0.087283	1.488355	-0.027226
18 = ES: all other	15.5	1.1	-0.110383	6.262899	-0.286055
19 = WS: all	54.180173	0.177962	-0.089253	1.533535	-0.028852
20 = AS: SM,SP	14.187987	0.416525	-0.126806	1.310744	-0.245126
20 = AS: all other	-2.04	1.4534	-0.058112	1.894400	-0.192979
21 = CO: SM,SP	14.187987	0.416525	-0.126806	1.310744	-0.245126
21 = CO: all other	-2.04	1.4534	-0.058112	1.894400	-0.192979
22 = OA: ***					
23 = OS: all	42.269377	0.	-0.165687	1.184734	0.
24 = OH: SM,SP	14.187987	0.416525	-0.126806	1.310744	-0.245126
24 = OH: all other	-2.04	1.4534	-0.058112	1.894400	-0.192979

Coefficients shown as blanks are equal to zero.

\*\*uses equations from another variant; described below

\*\*\*uses the equations described for the small tree model for all sized trees

Five species use large tree height growth relationships from other variants, to estimate uneven-aged height growth. These relationships predict height growth directly. The grand fir equation is from the Central Idaho variant. Equations for mountain hemlock, western red cedar, and western larch are from the North Idaho variant for elevation 6000 feet and habitat type set to 710 (TSME/XETE), 550 (THPL/OPHO), and 260 (PSME/PHMA) respectively. The limber pine equation is from the Utah variant. The equation form for four of these species is shown in {45} with species specific coefficients shown in Table 16.

$$\{45\} \text{ HTG} = \text{EXP}[\text{CON} + a_4 * \text{LN}(\text{DG})] + 0.4809$$

$$\text{CON} = a_0 + a_1 * \text{HT}^2 + a_2 * \text{LN}(\text{DBH}) + a_3 * \text{LN}(\text{HT})$$

where: HT = total tree height  
 LN = natural logarithm  
 DBH = tree diameter at breast height  
 DG = diameter growth for the tree

Table 16. Coefficients for calculating large tree height growth in the Central Rockies FVS variant, for species using equations from other variants for uneven-aged height growth estimate

Coefficient	Grand Fir	Mtn hemlock	W Red Cedar	W Larch
a <sub>0</sub>	1.38455	1.09510	1.21694	1.96089
a <sub>1</sub>	-0.00013358	-0.0000446	-0.00003631	-0.00002607
a <sub>2</sub>	-0.09775	-0.09775	-0.1219	-0.3899
a <sub>3</sub>	0.23315	0.23315	0.23315	0.23315
a <sub>4</sub>	0.62144	0.34003	0.37042	0.75756

Once uneven-aged height growth is estimated using equation {45}, it is adjusted for site index using equation {46} and the coefficients shown in Table 17.

$$\{46\} \text{HTG} = \text{HTG} * [a + b * \text{SI}]$$

where SI = site index, and site index is bounded to the range shown in Table 17 and the adjustment factor [a + b \* SI] is bounded to be 1.0 or greater for Western Red Cedar

Table 17. Coefficients for adjusting the large tree uneven-aged height growth estimate in the Central Rockies FVS variant for site index.

Coefficient	Grand Fir (SI ≤ 80)	Grand Fir (SI > 80)	Mtn hemlock	W Red Cedar	Western Larch	Limber Pine (SI < 40)	Limber Pine (SI ≥ 40)
a	0.1	-0.7	0.36	0.0875	0.23337	0.2	-0.1
b	0.0125	0.0225	0.012	0.01375	0.008333	0.015	0.0225
SI lower bound	40	40	40	40	40	20	20
SI upper bound	120	120	70	110	120	60	60

The equation for limber pine predicts future height and is more complex. If the beginning of cycle diameter or end of cycle diameter are greater than 45.1 or the beginning of cycle height is greater than 94.5 then height growth is set to 0.1 foot. If the tree dimensions are smaller than those limits, then the following set of equations is used:

$$Y1 = (\text{DBH} - 0.1) / 45$$

$$Y2 = (\text{HT} - 4.5) / 90$$

$$\text{FBY1} = \text{LN}[Y1 / (1 - Y1)]$$

$$\text{FBY2} = \text{LN}[Y2 / (1 - Y2)]$$

$$Z = [0.30546 + 0.94823 * \text{FBY2} - 0.70453 * (1.64770 + 1.35015 * \text{FBY1})] * 1.40910$$

$$\text{PSI} = 2.46480 * [(\text{D10} - 0.1) / (45.1 - \text{D10})]^{1.00316} * [e^{(0.74842 * Z)}]$$

$$\text{H10} = [(\text{PSI} / (1 + \text{PSI})) * 90] + 4.5$$

$$\begin{aligned} \text{HTG} &= \text{H10} - \text{HT} && \text{if } \text{H10} > \text{HT} \\ &= 0.1 && \text{otherwise} \end{aligned}$$

where DBH = beginning of cycle diameter  
 HT = beginning of cycle height  
 D10 = end of cycle diameter  
 H10 = end of cycle height

Height growth is then adjusted for site index using equation {46} and the coefficients shown in Table 17.

#### 4.6.2.3 COMBINING THE ESTIMATES INTO THE FINAL HEIGHT GROWTH ESTIMATE

As stated at the beginning of this section, the GENGYM equations predict height rather than height growth. In addition, there is an even-aged height estimate and an uneven-aged height estimate corresponding to the beginning of the growth cycle conditions and the end of the growth cycle conditions. These need to be combined to form the final height growth estimate.

The first step in this process, for model types other than the Black Hills, is to take the difference of the estimates to form the two height growth estimates {47} and {48}.

$$\{47\} \text{ HTGE} = \text{HTE10} - \text{HTEnow}$$

$$\{48\} \text{ HTGU} = \text{HTU10} - \text{HTUnow}$$

where HTGE is the even-aged height growth estimate  
 HTGU is the uneven-aged height growth estimate  
 HTEnow is the even-aged height estimate using beginning of cycle tree age  
 HTE10 is the even-aged height estimate using beginning of cycle tree age + 10 years  
 HTUnow is the uneven-aged height estimate using beginning of cycle values  
 HTU10 is the uneven-aged height estimate using end of cycle values (10 year cycle)

For the Black Hills model type, HTGE was already determined {36} and {37} and HTGU is estimated using {48}.

The second step in the process is to adjust the even-aged estimate for the Lodgepole Pine model type for young trees. This is necessary so the even-aged estimates match the site curve at age 30. If the tree age is less than 30, then even-aged height growth is estimated using equation {49}.

$$\{49\} \text{ HTGE} = [(5.25621 + 0.37515 * \text{SI} - 0.00082 * \text{CCF} * \text{SI}) * (\text{AGE}/31)] - \text{HT}$$

where SI = site index  
 CCF = crown competition factor for the inventory point on which the tree is located  
 AGE = current tree age  
 HT = beginning of cycle tree height

The third step is to multiply the even-aged estimate by a species specific adjustment factor so the trees will go through the site height. This is done for all model types using equation {50} and the factors shown in Table 18.

$$\{50\} \text{ HTGE} = \text{HTGE} * \text{FACTOR}$$

Table 18. Even-aged height growth adjustment factors for the Central Rockies FVS variant.

FVS Number = Alpha Code	SM model type FACTOR	SP model type FACTOR	BH model type FACTOR	SF model type FACTOR	LP model type FACTOR
1 = AF	1.25	1.25	1.13	1.15	1.25
2 = CB	1.25	1.25	1.13	1.15	1.25
3 = DF	1.18	1.18	1.10	1.18	1.25
4 = GF	1.00	1.00	1.10	1.00	1.10
5 = WF	1.20	1.20	1.13	1.15	1.25
6 = MH	1.00	1.00	1.10	1.00	1.10
7 = RC	1.00	1.00	1.10	1.00	1.10
8 = WL	1.00	1.00	1.10	1.00	1.10
9 = BC	1.00	1.00	1.00	1.00	1.00
10 = LM	1.00	1.00	1.07	1.00	1.07
11 = LP	1.20	1.15	1.13	1.10	1.30
12 = PI	1.00	1.00	1.00	1.00	1.00
13 = PP	1.20	1.20	1.10	1.15	1.25
14 = WB	1.20	1.15	1.10	1.05	1.20
15 = WP	1.20	1.20	1.10	1.15	1.20
16 = JU	1.00	1.00	1.00	1.00	1.00
17 = BS	1.20	1.20	1.15	1.10	1.20
18 = ES	1.20	1.20	1.15	1.10	1.20
19 = WS	1.20	1.20	1.15	1.10	1.20
20 = AS	1.00	1.00	1.00	1.00	1.00
21 = CO	1.15	1.15	1.05	1.05	1.18
22 = OA	1.00	1.00	1.00	1.00	1.00
23 = OS	1.15	1.15	1.05	1.05	1.15
24 = OH	1.15	1.15	1.15	1.05	1.20

The fourth step is to combine the even-aged and uneven-aged estimates if certain conditions are met. The even-aged height growth estimate is used: 1) if the stand is even-aged (range in tree ages is less than or equal to 40 years), 2) if the stand is uneven-aged and the total stand basal area is less than 70 square feet (open grown condition), or 3) if the stand is uneven-aged and the tree's percentile in the basal area distribution is 40 or greater (overstory tree). The uneven-aged estimate is used if the stand is uneven-aged and the tree's percentile in the basal area distribution is 10 or less (overtopped tree). For trees in an uneven-aged stand and their percentile in the basal area distribution is between 10 and 40, the even-aged and uneven-aged estimates are weighted using equation {51}.

$$\{51\} \text{HTG} = \text{XWT} * \text{HTGE} + (1 - \text{XWT}) * \text{HTGU}$$

$$\text{where XWT} = [(\text{PCT}-10) * 3.33333] / 100$$

and PCT is the tree's percentile in the basal area distribution  
HTG is the final height growth estimate  
HTGE is the even-aged height growth estimate  
HTGU is the uneven-aged height growth estimate

And finally, for aspen, the height growth estimate is adjusted for site index using equation {46} with a = 0.6253, b = 0.00583, and the site index bounds being 30 and 90.

#### 4.6.2.4 FINAL ADJUSTMENTS

Whether the height growth estimate was derived via a direct estimate using equations from another variant, or via the GENGYM method, some final adjustments need to be made. First a small random increment is added to the height growth to allow for some variability between individual trees. Second, a check is made to ensure that the height growth is not negative. Third, the height growth is adjusted to match the cycle length and account for any user-supplied height growth modifiers. And finally, if the stagnation effect has been activated, then its effects are accounted for using equation {52}.

$$\{52\} \text{ HTG} = \text{HTG} * (\text{DSTAG} + 1) / 2$$

For bristlecone pine, pinyon pine, juniper, and oaks, this section does not apply. The equations described in the small tree model section are used for trees of all sizes for these species.

### 4.6.3 Large Tree Crown Ratio Change

All species except mountain hemlock, western red cedar, and western larch use equations from GENGYM which predict crown length as a function of tree and stand attributes {53}, with coefficients shown in Table 19. Crown length is then converted to crown ratio by dividing crown length by total tree height.

$$\{53\} \text{ CL} = a_0 + a_1 * \text{HT} + a_2 * \text{DBH} + a_3 * \text{BA} + a_4 * \text{BAU}$$

where CL = predicted crown length

HT = total tree height

DBH = diameter at breast height

BA = total stand basal area

BAU = total stand basal area above the diameter class for the given tree

$a_0 - a_4$  are coefficients shown in Table 19

Table 19. Coefficients to predict crown length for the Central Rockies FVS variant.

FVS Number = Alpha Code: Model Type	$a_0$	$a_1$	$a_2$	$a_3$	$a_4$
1 = AF; SW, SP	0.50706	0.73070			
1 = AF; all others	0.36135	0.57085			
2 = CB; SW,SP	0.50706	0.73070			
2 = CB; all others	0.36135	0.57085			
3 = DF; all	6.47479	0.50703	0.54482	-0.03326	
4 = GF; all	6.22959	0.67587		-0.03098	
5 = WF; all	6.22959	0.67587		-0.03098	
6 = MH; all	See equation {54}				
7 = RC; all	See equation {55}				
8 = WL; all	See equation {56}				
9 = BC; all	-0.59373	0.67703			
10 = LM; all	-0.59373	0.67703			
11 = LP; all	5.00215	0.06334	0.88236		-0.03821
12 = PI; all	-0.59373	0.67703			
13 = PP; SW	5.63367	0.56252		-0.06411	
13 = PP; SP	4.35671	0.32549	0.84714	-0.03802	
13 = PP; all others	3.49178	0.17421	0.80767	-0.03272	
14 = WB; all	-0.59373	0.67703			
15 = WP; all	3.03832	0.65587		-0.01792	

16 = JU; all	-0.59373	0.67703		
17 = BS; all	3.61635	0.61547	0.93639	-0.02360
18 = ES; SW, SP	1.05857	0.68442		
18 = ES; all other	3.22244	0.44315	0.44755	
19 = WS; all	0.15768	0.74697		
20 = AS; all	5.17281	0.32552		-0.01675
21 = CO; all	5.17281	0.32552		-0.01675
22 = OA; all	-0.59373	0.67703		
23 = OS; all	-0.59373	0.67703		
24 = OH; all	5.17281	0.32552		-0.01675

Coefficients shown as blanks are equal to zero

The remaining three species use equations from other variants that predict crown ratio directly. The equation for mountain hemlock is given in {54} with coefficients shown in Table 19. This equation is from the North Idaho variant for the Bitterroot National Forest with habitat type set to 710.

$$\{54\} CR = 0.3450 - 0.00264 * BA + 0.00000512 * CCF^2 - 0.25138 * LN(HT) + 0.05140 * LN(PCT)$$

where CR = predicted crown ratio

BA = total stand basal area

CCF = total stand crown competition factor

HT = total tree height at the beginning of the cycle

PCT = the trees percentile in the basal area distribution

LN = natural logarithm

The equation for western red cedar is shown in equation {55} with coefficients shown in Table 19. This equation is from the North Idaho variant with habitat type set to 550.

$$\{55\} CR = -1.6053 + 0.17479 * LN(BA) - 0.00183 * CCF - 0.00560 * DBH + 0.11050 * LN(PCT)$$

where DBH = tree diameter at breast height at the end of the cycle

and all other variables are as defined above

The equation for western larch is shown in equation {56} with coefficients shown in Table 19. This equation is also from the North Idaho variant for the Bitterroot National Forest with habitat type set to 260.

$$\{56\} CR = 0.03441 - 0.00204 * BAT + 0.30066 * LN(DBH) - 0.59302 * LN(HT)$$

Once crown ratio is predicted, it is bounded to a change of no more than ten percent per cycle, and to no more than the potential change in crown ratio if all the height growth contributed to the crown change during the cycle.

## **4.7 MORTALITY MODEL**

The mortality model used in the Central Rockies variant is based on Stand Density Index (SDI), and techniques developed by Dixon (1986). The mortality model imbedded in the GENGYM model was used in earlier versions of this variant, but it did not perform as well as desired. The new mortality model should provide users with the flexibility they want in manipulating mortality, as well as the model sensitivity they need to simulate stand conditions that change through time.

Two types of mortality are present: (1) background mortality, and (2) density related mortality. Density related mortality accounts for mortality in stands that are dense enough for competition to be the causal agent. All other mortality is attributable to background mortality. Background mortality gives way to density related mortality based on the relationship between current and maximum stand SDI. In the Central Rockies variant, density related mortality begins when the stand SDI is above 55 percent of maximum SDI, and stand density peaks at 85 percent of maximum SDI (Smith 1984, Long 1984). Users can change these values using fields 5 and 6 of the SDIMAX keyword. Background mortality is used when current stand SDI is below 55 percent of maximum SDI. The 55 percent value is referred to as the lower limit of density related mortality, and the 85 percent value is the upper limit.

Users can set maximum SDI values for any, or all, species with the SDIMAX keyword, or the default values shown in Table 6 will be used. The stand SDI maximum is a weighted average {57} of the individual species SDI maximums. The weights are based on the basal area each individual species represents in the stand. The weighted maximum SDI is calculated each growth cycle, and mortality is determined based on the stands' position relative to the maximum SDI. Over time, maximum SDI changes as the species mix in the stand changes.

$$\{57\} \text{ Maximum SDI} = \frac{S1SDI*S1BA + S2SDI*S2BA + \dots + SnSDI*SnBA}{\text{TOTAL STAND BA}}$$

where S1SDI = maximum SDI for the first species in the stand  
 S1BA = total basal area of species 1 in the stand  
 S2SDI = maximum SDI for the second species in the stand  
 S2BA = total basal area of species 2 in the stand  
 SnSDI = maximum SDI for the nth species in the stand  
 SnBA = total basal area of the nth species in the stand

Current stand SDI is calculated using equation {58} (Long and Daniel 1990).

$$\{58\} \text{ Stand SDI} = \Sigma[\text{TPA}_i * (\text{DBH}_i/10)^{1.605}]$$

where TPA<sub>i</sub> = trees-per-acre represented by the i<sup>th</sup> tree record  
 DBH<sub>i</sub> = diameter at breast height of the i<sup>th</sup> tree record  
 and the summation is over all trees in the stand

A restriction on DBH was added in FVS to achieve mathematical consistency with a similar estimate based on stand values. For trees with a diameter less than 1.0 inch, a diameter of 1.0 inch is used in the calculation.

If the stand SDI at the time of inventory is above the upper limit of density related mortality plus 5 percent (e.g. 90% if using the default value of 85% for the upper limit), then the maximum SDI is automatically reset. The new maximum is set so the stand SDI at the time of inventory corresponds to the upper limit of density related mortality. If the stand SDI at the time of inventory is greater than the upper limit of density related mortality, but within 5 percent, then the stand stocking will be reduced to the upper limit the first projection cycle.

The relationship between stand SDI at the time of inventory and the maximum SDI determines the trajectory a stand will take throughout the projection. Certain management actions, such as a thinning, may change this trajectory. This trajectory can be thought of as a relationship between trees-per-acre on the y-axis and quadratic mean diameter on the x-axis. For density related mortality, this trajectory determines how many trees will die in the projection cycle. For background mortality, the number of trees dying is determined by the background mortality rate.

The background mortality rates in the Central Rockies variant were not available. Those fit for the Southern Oregon / Northeast California (SO) variant are used. Species in the Central Rockies variant use coefficients from the most similar species in the SO variant for which coefficients were estimated. The background rate, equation {59}, is an annual mortality rate that is adjusted to the projection cycle length using a compound interest formula {60}. Coefficients for species in the CR variant are shown in Table 20.

$$\{59\} RI = (1 / [1 + e^{(a + b \cdot DBH)}]) / 2$$

where RI = annual background mortality rate  
DBH = tree diameter at breast height

$$\{60\} RIP = 1 - [1 - RI]^{YRS}$$

where RIP = background mortality rate for the current projection cycle  
YRS = number of years in the current projection cycle

Table 20. Coefficients for the background mortality equation in the Central Rockies variant

a	b	Central Rockies Species
6.5112	-0.0052485	WL, WP
7.2985	-0.0129121	DF
5.1677	-0.0077681	AF, CB, GF, WF, RC, BC, LM, PI, WB, JU, OS
9.6943	-0.0127328	MH, BS, ES, WS
5.9617	-0.0340128	LP, AS, CO, OA, OH
5.5877	-0.005348	PP

Once the number of mortality trees has been determined, the mortality needs to be dispersed across the individual tree records. Mortality in FVS is achieved by adjusting the number of trees-per-acre a record represents. Tree records are processed, each receiving a calculated mortality, until the total number of mortality trees has been achieved. All tree records will receive some mortality in a projection.

Mortality rates for individual tree records in the Central Rockies variant, equation {61}, are partially dependent on shade tolerance of individual species. The more intolerant species have higher mortality rates than the tolerant species. Shade tolerance ratings for species in the CR variant are shown in Table 21, where 0.1 corresponds to a species being very tolerant, 0.3 tolerant, 0.5 moderately tolerant, 0.7 intolerant, and 0.9 very intolerant. The rate is also dependent on a tree's social position as measured by its' rank in the basal area distribution. Tree's with a lower rank (e.g. understory tree) receive heavier mortality than those with a higher rank (e.g. overstory tree). And finally, the rate is dependent on a tree's vigor as measured by crown ratio. Trees with a lower crown ratio receive higher mortality than trees with a higher crown ratio. The mortality model makes multiple passes through the tree records multiplying a record's trees-per-acre value times the mortality rate (MR), accumulating the results, and reducing the trees-per-acre representation until the desired mortality level has been reached.

$$\{61\} MR = [0.84525 - 0.01074 * PCT + 0.0000002 * PCT^3] * [(100 - CR)/100] * SHADE * 0.01$$

where MR = individual tree mortality rate  
PCT = a tree's percentile rank in the basal area distribution  
CR = a tree's crown ratio  
SHADE = a tree's shade tolerance rating (shown in Table 21)  
(and the value of the function in the first bracket is bounded between 0.01 and 1.0)

Table 21. Shade tolerance ratings used in the mortality function for the Central Rockies FVS variant.

FVS Number = Alpha Code	SHADE
1 = AF	0.1
2 = CB	0.1
3 = DF	0.5
4 = GF	0.3
5 = WF	0.3
6 = MH	0.3
7 = RC	0.1
8 = WL	0.9
9 = BC	0.9
10 = LM	0.9
11 = LP	0.7
12 = PI	0.7
13 = PP	0.7
14 = WB	0.9
15 = WP	0.5
16 = JU	0.7
17 = BS	0.5
18 = ES	0.3
19 = WS	0.3
20 = AS	0.9
21 = CO	0.9
22 = OA	0.7
23 = OS	0.7
24 = OH	0.9

## 5.0 VOLUME ESTIMATION

The Central Rockies variant contains a choice of three volume estimation methods. These are (1) volume equations contained in the National Volume Estimator Library; (2) southwestern volume equations; and (3) user defined volume equations. The National Volume Estimator Library contains equations from a variety of sources and is generally regarded as the “standard” for use in the Forest Service. Southwestern volume equations are from Chojnacky and Ott (1986) for Pinyon and Juniper, Chojnacky (1988) for oaks, and Hann and Bare (1978) for the remaining species.

For Region 2 forests, the default is the National Volume Estimator Library equations. If a user on a Region 2 forest chooses to use the southwestern equations, then equation coefficients for the Cibola National Forest are used.

For Region 3 forests, the default is the southwestern equations because the National Volume Estimator Library equations for Region 3 currently only returns merchantable cubic and board foot volumes and not total cubic foot volume.

Volume adjustments such as adjusting the merchantable top diameters, minimum diameter for merchantability, and defect adjustments can be made using the VOLUME, BFVOLUME, BFFDLN, BFDEFECT, MCFDLN, and MCDEFECT keywords. Individual tree defect percentages can also be entered directly in the tree data.

### **5.1 NATIONAL VOLUME ESTIMATOR LIBRARY EQUATIONS**

Equation numbers for the National Volume Estimator Library equations are given in Table 22. For Region 2, if the equation number is blank, volumes are not calculated for that species. There are exceptions to the equation numbers shown in Table 22. Some of these exceptions are based on model type, and some are based on National Forest codes.

Exceptions to the equation numbers presented in Table 22 are as follows:

- (1) The Southwest Ponderosa Pine model type uses Region 3 equation number 304 for subalpine fir, corkbark fir, and grand fir.
- (2) The Black Hills model type uses Region 2 equation number 200CZ2W746 for cottonwood.
- (3) The Spruce-fir model type uses Region 3 equation number 306 for white fir.
- (4) The Lodgepole pine model type uses Region 3 equations 306 for white fir and 307 for lodgepole pine.
- (5) The Black Hills National Forest uses Region 2 equation number 203FW2W122 for ponderosa pine.
- (6) The San Juan National Forest uses Region 2 equation number 213FW2W122 for ponderosa pine.
- (7) The Big Horn and Shoshone National Forests use Region 2 equation number 202FW2W108 for lodgepole pine.
- (8) The Carson and Sante Fe National Forests use Region 3 equation numbers 303 for Douglas-fir and 305 for white fir in the Southwest Mixed Conifer model type, and the Black Hills model type.
- (9) The Carson and Sante Fe National Forests use Region 3 equation numbers 303 for Douglas-fir and Grand fir, and 305 for white fir, subalpine fir, and corkbark fir in the Southwest Ponderosa Pine model type.
- (10) The Carson National Forest uses equation 303 for Douglas-fir in the Spruce-fir model type.

Table 22. National Volume Estimator Library equation numbers for the Central Rockies FVS variant.

FVS Number = Alpha Code	Region 2 Equation Number	Region 3 Equation Number
1 = AF	200CZ2W019	306
2 = CB	200CZ2W019	306
3 = DF	200CZ2W202	302
4 = GF	200CZ2W019	306
5 = WF	200CZ2W015	304
6 = MH	407FW2W093	307
7 = RC	407FW2W093	306
8 = WL	407FW2W093	306
9 = BC	200CZ2W122	307
10 = LM	200CZ2W122	307
11 = LP	200FW2W108**	307
12 = PI		310
13 = PP	200CZ2W122*	301
14 = WB	200CZ2W122	307
15 = WP	200CZ2W122	307
16 = JU		309
17 = BS	407FW2W093	306
18 = ES	407FW2W093	306
19 = WS	407FW2W093	306
20 = AS	200CZ2W746	308
21 = CO		311
22 = OA		312
23 = OS		309
24 = OH		311

## 5.2 SOUTHWESTERN VOLUME EQUATIONS

Total cubic foot volume for Pinyon and Juniper are calculated using equations from Chojnacky and Ott (1986), and total cubic foot volume for oak is calculated using equations from Chojnacky (1988). In the FVS output report, merchantable cubic foot volume is set equal to total cubic foot volume for these species, since these species are primarily used for firewood. Board foot volumes for these species are not computed. The equation form is shown in {62} with coefficients shown in Table 23.

$$\{62\} \quad V = a_0 + a_1 * X + a_2 * X^2 \quad \text{for } X \leq 5$$

$$V = b_0 + b_1 * X - b_2 / X \quad \text{for } X > 5$$

where  $V$  = total cubic foot volume  
 $X = \text{DBH}^2 * \text{HT}$   
 $\text{DBH}$  = tree diameter at breast height  
 $\text{HT}$  = total tree height  
 $a_0 - a_2$  are coefficients shown in Table 23  
 $b_0 - b_2$  are coefficients shown in Table 23

Table 23. Coefficients for pinyon, juniper, and oak volumes in the southwestern equation set for the Central Rockies variant

Species	a <sub>0</sub>	a <sub>1</sub>	a <sub>2</sub>	b <sub>0</sub>	b <sub>1</sub>	b <sub>2</sub>
Pinyon	-0.07	2.51	0.098	7.29	2.51	24.53
Juniper	-0.05	2.48	0.057	4.24	2.48	14.29
Oak	-0.068	2.4048	0.1383	6.571	2.4048	17.704

Volumes for cottonwood and the miscellaneous categories “other softwoods” and “other hardwoods” are not computed.

Volumes for all other species are computed using equations from Hann and Bare (1978). Table 24 shows the equation index by species and National Forest, and Table 25 shows which Hann and Bare (1978) equation this corresponds to. For example, for species BC, the index value is 1 for all Region 3 forests. This indicates the Hann and Bare (1978) white pine equation is used to calculate volumes for this species.

Table 24. Southwestern volume equation index by Forest for the Central Rockies FVS variant.

FVS Number = Alpha Code	F O R E S T											all R2
	301	302	303	304	305	306	307	308	309	310	312	
1 = AF	2	2	2	2	2	2	2	2	2	2	2	2
2 = CB	2	2	2	2	2	2	2	2	2	2	2	2
3 = DF	6	7	7	7	7	7	7	6	7	7	7	7
4 = GF	2	2	2	2	2	2	2	2	2	2	2	2
5 = WF	9	10	10	10	10	10	10	9	10	10	10	10
6 = MH	9	10	10	10	10	10	10	9	10	10	10	10
7 = RC	9	10	10	10	10	10	10	9	10	10	10	10
8 = WL	9	10	10	10	10	10	10	9	10	10	10	10
9 = BC	1	1	1	1	1	1	1	1	1	1	1	1
10 = LM	1	1	1	1	1	1	1	1	1	1	1	1
11 = LP	6	7	7	7	7	7	7	6	7	7	7	7
12 = PI												
13 = PP	4	5	4	4	4	4	4	4	4	5	4	4
14 = WB	1	1	1	1	1	1	1	1	1	1	1	1
15 = WP	1	1	1	1	1	1	1	1	1	1	1	1
16 = JU												
17 = BS	2	2	2	2	2	2	2	2	2	2	2	2
18 = ES	2	2	2	2	2	2	2	2	2	2	2	2
19 = WS	2	2	2	2	2	2	2	2	2	2	2	2
20 = AS	8	8	8	8	8	8	8	8	8	8	8	8
21 = CO												
22 = OA												
23 = OS												
24 = OH												

\*Volume is not computed for species where the index is blank

Table 25. Hann and Bare (1978) equations used in the Central Rockies Variant

Index	Description
1	White Pine
2	Engelmann Spruce / Corkbark Fir
3	Yellow Pine
4	Ponderosa Pine - - Coconino, Tonto, Lincoln National Forests
5	Ponderosa Pine - - Santa Fe, Carson National Forests
6	Douglas-fir - - Lincoln, Tonto National Forests
7	Douglas-fir - - Santa Fe, Carson National Forests
8	Aspen
9	White Fir - - Lincoln National Forest
10	White Fir - - Santa Fe, Carson National Forests

Total cubic foot volumes are computed using equation {63} and coefficients shown in Table 26. Merchantable cubic foot volume is calculated using equations {64} and {65} and coefficients shown in Table 26.

$$\{63\} TV = a_0 + a_1 * DBH^2 * HT$$

where TV = total cubic foot volume  
 DBH = tree diameter at breast height  
 HT = total tree height  
 and  $a_0$  and  $a_1$  are shown in Table 26

$$\{64\} TOP = b_1 + [b_2 * TOPD^3 * HT] / [DBH^{b_0}] + b_3 * DBH^2$$

where TOP = total volume above the merchantable top  
 TOPD = merchantable top diameter inside bark for cubic foot volume  
 DBH = tree diameter at breast height  
 HT = total tree height  
 and  $b_0$ - $b_3$  are shown in Table 26

$$\{65\} VM = TV - TOP$$

where VM = total merchantable cubic foot volume

Table 26. Hann and Bare (1978) total cubic foot and merchantable cubic foot volume coefficients

Index	$a_0$	$a_1$	$b_0$	$b_1$	$b_2$	$b_3$
1	0.16089	0.0020325	1.5	-0.21301	0.0049121	0.0060606
2	0.22547	0.0021697	1.5	-0.26648	0.0061290	0.0074311
3	0.23720	0.0022112	1.0	0.01855	0.0007882	0.0050551
4	0.08107	0.0019835	1.5	-0.12535	0.0036042	0.0054063
5	0.04831	0.0020497	1.5	-0.13397	0.0065017	0.0049022
6	0.43837	0.0017564	1.0	-0.08315	0.0012190	0.0054174
7	0.34113	0.0019180	1.5	-0.18763	0.0067187	0.0053645
8	0.03270	0.0023112	1.5	-0.23643	0.0058021	0.0060804
9	0.21090	0.0018400	1.0	-0.18270	0.0012482	0.0062448
10	0.15778	0.0020091	1.5	-0.18756	0.0063265	0.0060413

Merchantable Scribner board foot volumes are computed using equations {63}, {64}, {66}, {67} and {68} and coefficients shown in Tables 26, 27, and 28. First, equation {64} is evaluated with BFTOPD replacing TOPD, where BFTOPD is the merchantable top diameter inside bark for board foot volume. Next, equations {66} through {68} are executed in order.

$$\{66\} \text{VMR} = \text{TV} - \text{TOP}$$

where TV is the total cubic foot volume {63} and TOP is the value of {64} with BFTOPD replacing TOPD

$$\{67\} \text{VI} = \text{VMR} * [f_0 - (f_1 / \text{DBH}) - (f_2 / \text{DBH}^2) - (f_3 / \text{DBH}^3)]$$

where VI = international board foot volume  
 DBH = tree diameter at breast height  
 and  $f_0 - f_3$  are shown in Table 27

$$\{68\} \text{VS} = \text{VI} * [e_0 - (e_1 / \text{DBH}) - (e_2 / \text{DBH}^{1.177748}) - (e_3 / \text{DBH}^2)]$$

where VS = Scribner board foot volume  
 DBH = tree diameter at breast height  
 VI = international board foot volume from equation {67}  
 and  $e_0 - e_3$  are shown in Table 28

Table 27. Hann and Bare (1978) International board foot volume coefficients

Index	$f_0$	$f_1$	$f_2$	$f_3$
1	6.69197	7.52011	216.34837	0.
2	5.98736	9.84792	-300.81281	2855.34246
3	7.10051	7.97922	229.55650	0.
4	6.84752	7.69491	221.37723	0.
5	7.58122	8.51941	245.09754	0.
6	6.58735	0.89272	243.51491	0.
7	6.59717	0.89405	243.87797	0.
8	6.68808	-1.27685	-4.50480	1423.98524
9	6.24688	7.01994	201.95873	0.
10	5.73645	1.72093	74.57379	0.

Table 28. Hann and Bare (1978) Scribner board foot volume coefficients

Index	$e_0$	$e_1$	$e_2$	$e_3$
1	1.00609	2.38466	0.	0.
2	0.87845	0.	0.	15.99846
3	0.98210	0.92603	0.	14.49444
4	0.96579	0.40579	0.	16.93678
5	0.99399	1.46349	0.	12.40585
6	1.00090	0.	4.10007	0.
7	0.87026	0.	0.	19.49594
8	0.88789	0.	0.	17.19374
9	1.0	1.88814	0.	8.85145
10	1.01725	1.87057	0.	8.51445

### **5.3 USER DEFINED VOLUME EQUATIONS**

A user's own volume equations can be used in FVS if they fit the functional form shown in equation {69}. Equation coefficients are entered into FVS using the CFVOLUME and/or BFVOLUME keywords. Users must also use the VOLUME and/or BFVOLUME keywords, and enter a volume calculation method of 7 in field 7 to tell FVS that user defined equations should be used in the calculation of volumes.

$$\{69\} V = a_0 + a_1 * DBH + a_2 * DBH * HT + a_3 * DBH^2 * HT + a_4 * DBH^{a_5} * HT^{a_6}$$

where V = volume  
DBH = tree diameter at breast height  
HT = total tree height  
a<sub>0</sub> – a<sub>6</sub> = user defined coefficients

## 6.0 REGENERATION ESTABLISHMENT

The FVS regeneration / establishment model is used to simulate stand establishment from bare ground, or to bring seedlings into a simulation with existing trees. Table 29 shows the bud width, minimum seedling heights, and maximum seedling heights by species for the Central Rockies variant.

Table 29. Bud widths and minimum seedling height for species in the Central Rockies FVS variant.

FVS Number = Alpha Code	Bud Width (inches)	Minimum Seedling Height (ft)	Maximum Seedling Height (ft)
1 = AF	0.3	0.5	7
2 = CB	0.3	0.5	7
3 = DF	0.3	1.0	10
4 = GF	0.3	0.5	7
5 = WF	0.3	0.5	7
6 = MH	0.3	0.5	10
7 = RC	0.3	0.5	9
8 = WL	0.3	1.0	10
9 = BC	0.4	0.5	9
10 = LM	0.4	0.5	9
11 = LP	0.4	1.0	10
12 = PI	0.4	0.5	6
13 = PP	0.5	1.0	10
14 = WB	0.4	1.0	9
15 = WP	0.4	1.0	9
16 = JU	0.3	0.5	6
17 = BS	0.3	0.5	7
18 = ES	0.3	0.5	7
19 = WS	0.3	0.5	7
20 = AS	0.2	3.0	16
21 = CO	0.3	3.0	16
22 = OA	0.3	0.5	10
23 = OS	0.2	1.0	9
24 = OH	0.2	0.5	12

The Central Rockies variant has three species that automatically produce stump sprouts when cut. These are aspen, cottonwood, and oak. Users wanting to turn the automatic sprouting off can do so with the NOSPROUT keyword. Establishment of all other species must be user specified with the PLANT or NATURAL keywords.

Two sets of equations are used to grow regenerating trees in height from the time they are established until the end of the cycle in which they are established. The first set estimates tree height five years after seedlings are established, or at the end of the cycle if the cycle boundary is within five years of the establishment date. The second set grows the trees from the point five years after establishment to the end of the cycle.

The first set of equations is still under development, and for now a height of 1.0 foot is assumed for all species. However, users can override this value by specifying an average seedling height in field 6 of the PLANT or NATURAL keywords. The height specified in field 6 is not subject to the minimum height restrictions shown in Table 29 and seedlings as small as 0.1 foot can be established.

The second set of equations, which grow the trees in height from the point five years after establishment to the end of the cycle, are the equations described in the section 4.5.1. After seedling height is estimated, diameter growth is estimated using equations described in section 4.5.2.

Regenerating trees become visible in FVS at the end of the growth cycle. FVS automatically generates tree records corresponding to regenerating trees. These tree records can be found in the tree list output file with tree identification numbers beginning with the letters "ES".

## **7.0 FIRE AND FUELS EXTENSION**

The fire and fuels extension to FVS (Beukema et.al. 1998) integrates FVS with elements from existing models of fire behavior and fire effects. It also simulates silvicultural impacts on fuel pools, and tracks snags from the time the tree dies until it falls over and decays. Various types of fuels are represented, including ladder and canopy fuels, and surface fuels. Fire behavior and fire effects on the stand are modeled.

The fire and fuels extension does not simulate fire spread or the probability of fire. However, given that a fire does occur, the model will predict the potential fire intensity, resulting mortality, and various other fire-related effects. Model outputs include displays of fuel loading, stand structure, snags, and potential fire behavior over time. The fire and fuels extension, coupled with capabilities of FVS, provides a basis for comparing proposed fuel treatments.

The snag and woody debris portion of the model is useful without invoking any fire simulations. The predicted quantity and dynamics of standing and downed dead wood are of interest to wildlife biologists and forest managers. A detailed description of the fire and fuels extension can be found in Beukema et.al. (1998).

## 8.0 LITERATURE CITED

- Alexander, R.R. 1967. Site indexes for Engelmann spruce. USDA Forest Service Rocky Mountain Forest and Range Experiment Station. Fort Collins, CO. Res Paper RM-32. 7p.
- Alexander, R.R.; D. Tackle; W.G. Dahms. 1967. Site indexes for lodgepole pine with corrections for stand density: Methodology. USDA Forest Service Rocky Mountain Forest and Range Experiment Station. Fort Collins, CO. Res Paper RM-29. 18p.
- Beukema, S.J., E.Reinhardt, J.A. Greenough, W.A. Kurtz, N. Crookston, and D.C.E. Robinson. 1998. Fire and fuels Extension: model description, working draft. Prepared by ESSA Technologies Ltd., Vancouver, BC for USDA Forest Service, Rocky Mountain Research Station, Missoula, MT, 58pp.
- Chojnacky, David C. 1988. Juniper, pinyon, oak, and mesquite volume equations for Arizona. USDA Forest Service Intermountain Research Station. Ogden, UT. Res Paper INT-391.
- Chojnacky, David C. and Janet S. Ott. 1986. Pinyon-juniper volume equations for Arizona Hualapai and Havasupai Indian reservations. USDA Forest Service Intermountain Research Station. Ogden, UT. Res Note INT-363. 4p.
- Clark, Alexander III; Ray A. Souter; and Bryce E. Schlaegel. 1991. Stem profile equations for Southern tree species. USDA Forest Service Southeastern Forest Experiment Station. Asheville, NC. Res Paper SE-282. 113p.
- Dixon, Gary E. 1986. Prognosis mortality modelling. USDA Forest Service Washington Office Forest Management Service Center. Fort Collins, CO. Internal Report on file.
- Dolph, K. Leroy. 1984. Relationships of inside and outside bark diameters for young-growth mixed-conifer species In the Sierra Nevada. Res. Note PSW-368. Berkeley, CA: Pacific Southwest Forest and Range Experiment Station, Forest Service, U.S. Department of Agriculture. 4p.
- Edminster, Carleton B.; James R. Getter; and Donna R. Story. 1977. Past diameters and gross volumes of Plains cottonwood in Eastern Colorado. USDA Forest Service Rocky Mountain Forest and Range Experiment Station. Fort Collins, CO. Res Note RM-351. 4p.
- Edminster, C.B.; R.L. Mathiasen; and W.K. Olsen. 1991. A method for constructing site index curves from Height-age measurements applied to Douglas-fir in the Southwest. USDA Forest Service Rocky Mountain Forest and Range Experiment Station. Fort Collins, CO. Res. Note RM-510. 6p.
- Edminster, Carleton B.; H. Todd Mowrer; Robert L. Mathiasen; et. al. 1991. GENGYM: A variable density stand table projection system calibrated for mixed conifer and ponderosa pine stands in the Southwest. USDA Forest Service Rocky Mountain Forest and Range Experiment. Station. Fort Collins, CO. Res. Paper RM-297. 32p.
- Hann, David W. and B. Bruce Bare. 1978. Comprehensive tree volume equations for major species of New Mexico and Arizona: II. Tables for unforked trees. USDA Forest Service Intermountain Forest and Range Experiment Station. Ogden, UT. Res Paper INT-210. 127p.
- Johnson, Barry C. 1987. Plant associations of Region two: potential communities of Wyoming, South Dakota, Nebraska, Colorado, and Kansas, Edition 4. USDA Forest Service. Report R2-ECOL-87-2.
- Long, James. 1984. Personal communication. Utah State University, Logan, UT
- Long, J.N. and T.W. Daniel. 1990. Assessment of growing stock in uneven-aged stands. West. J. Appl. For. 5:93-96.

- Meyer, W.H. 1961 rev. Yield of even-aged stands of ponderosa pine. US Department of Agriculture. Technical Bulletin No. 630. 59p.
- Minor, C.O. 1964. Site-index curves for young-growth ponderosa pine in Northern Arizona. USDA Forest Service Rocky Mountain Forest and Range Experiment Station. Fort Collins, CO. Res Note RM-37. 8p.
- Myers, Clifford A. 1964. Taper tables, bark thickness, and diameter relationships for lodgepole pine in Colorado And Wyoming. USDA Forest Service Rocky Mountain Forest and Range Experiment Station. Fort Collins, CO. Res Note RM-31. 6p.
- Myers, Clifford A.; and Robert R. Alexander. 1972. Bark thickness and past diameters of Engelmann spruce in Colorado and Wyoming. USDA Forest Service Rocky Mountain Forest and Range Experiment Station. Fort Collins, CO. Res Note RM-217. 2p.
- Myers, Clifford A.; and James L. Van Deusen. 1958. Estimating past diameters of ponderosa pine in the Black Hills. USDA Forest Service Rocky Mountain Forest and Range Experiment Station. Fort Collins, CO. Res Note No 32. 2p.
- Schmidt, Wyman C., Raymond C. Shearer, and Arthur L. Roe. 1976. Ecology and silviculture of western larch Forests. USDA Forest Service Technical Bulletin No 1520. 96p.
- Shepperd, Wayne D. 1995. Unpublished equation. Data on file, RMRS. USDA Forest Service Rocky Mountain Research Station. Fort Collins, CO.
- Smith, Frederick (Skip). 1984. Personal communication. Colorado State University, Fort Collins, CO.
- Stage, A. R. 1973. Prognosis model for stand development. USDA Forest Service Intermountain Forest and Range Experiment Station. Ogden, UT. Res. Paper INT-137. 32p.
- USDA Forest Service. 1997. Plant associations of Arizona and New Mexico, Volume 1: forests, Volume 2: woodlands, Edition 3. USDA Forest Service Southwestern Region. Habitat Typing Guides. V 1: 291p, V 2: 196p.
- USDA Forest Service. 2000. Common Stand Exam Appendices. USDA Forest Service Ecosystems Management Staff. Fort Collins, CO. Internal Report Version 1.4, April 2000.
- Wykoff, William R., Nicholas L. Crookston, and Albert R. Stage. 1982. User's guide to the stand prognosis model. USDA Forest Service Intermountain Forest and Range Experiment Station. Ogden, UT. General Technical Report INT-133. 112p.

## 9.0 APPENDICES

### APPENDIX A: REGION 2 PLANT ASSOCIATION CODES FOR THE CENTRAL ROCKIES VARIANT

200101	White fir-Douglas-fir/Rocky Mountain maple
2001010	White fir-Douglas-fir/Rocky Mountain maple/Rocky Mountain Maple
2001011	White fir-Douglas-fir/Rocky Mountain maple/Oregon-grape
2001012	White fir-Douglas-fir/Rocky Mountain maple/ocean spray
2001013	White fir-Douglas-fir/Rocky Mountain maple/thinleaf alder
200102	White fir-Douglas-fir/sparse undergrowth
200103	White fir-Douglas-fir/forest fleabane
200104	White fir-Douglas-fir/Arizona fescue
2001040	White fir-Douglas-fir/Arizona fescue/Arizona fescue
2001041	White fir-Douglas-fir/Arizona fescue/Parry oatgrass
200105	White fir-Douglas-fir/Gambel oak
2001050	White fir-Douglas-fir/Gambel oak/Gambel oak
2001052	White fir-Douglas-fir/Gambel oak/Arizona fescue
2001053	White fir-Douglas-fir/Gambel oak/fragrant bedstraw
2001054	White fir-Douglas-fir/Gambel oak/mountain lover
200109	White fir-Douglas-fir/bearberry
200110	White fir-Douglas-fir/Rocky Mountain whortleberry
200111	White fir-Douglas-fir/Saskatoon serviceberry
200112	White fir-Douglas-fir/greenleaf manzanita
200113	White fir-Douglas-fir/ocean spray
200114	White fir-Douglas-fir/mountain snowberry
200115	White fir-limber pine/Arizona fescue
200116	White fir-Douglas-fir/common juniper
200117	White fir-Douglas-fir/Oregon-grape
200118	White fir-Douglas-fir/mallow ninebark
200201	Subalpine fir/elk sedge
200203	Subalpine fir/mountain lover
200301	Subalpine fir-Engelmann spruce/red baneberry
200302	Subalpine fir-Engelmann spruce/heartleaf arnica

2003020 Subalpine fir-Engelmann spruce/heartleaf arnica/heartleaf arnica  
 2003021 Subalpine fir-Engelmann spruce/heartleaf arnica/weedy milkvetch  
 2003022 Subalpine fir-Engelmann spruce/heartleaf arnica/russet buffaloberry  
 2003023 Subalpine fir-Engelmann spruce/heartleaf arnica/Engelmann spruce  
 200303 Subalpine fir-Engelmann spruce/broadleaf arnica  
 200304 Subalpine fir-Engelmann spruce/Oregon-grape  
 200305 Subalpine fir-Engelmann spruce/bluejoint reedgrass  
 200306 Subalpine fir-Engelmann spruce/mountain bluebells  
 200307 Subalpine fir-Engelmann spruce/elk sedge  
 200308 Subalpine fir-Engelmann spruce/forest fleabane  
 200309 Subalpine fir-Engelmann spruce/common juniper  
 200310 Subalpine fir-Engelmann spruce/American twinflower  
 2003100 Subalpine fir-Engelmann spruce/American twinflower/American twinflower  
 2003101 Subalpine fir-Engelmann spruce/American twinflower/broom huckleberry  
 200311 Subalpine fir-Engelmann spruce/moss species  
 200313 Subalpine fir-Engelmann spruce/mountain lover  
 2003130 Subalpine fir-Engelmann spruce/mountain lover/mountain lover  
 2003131 Subalpine fir-Engelmann spruce/mountain lover/Douglas-fir  
 2003132 Subalpine fir-Engelmann spruce/mountain lover/mountain gooseberry  
 200315 Subalpine fir-Engelmann spruce/Wheeler bluegrass  
 200316 Subalpine fir-Engelmann spruce/arrowleaf groundsel  
 200318 Subalpine fir-Engelmann spruce/western meadow-rue  
 200319 Subalpine fir-Engelmann spruce/globe huckleberry  
 2003190 Subalpine fir-Engelmann spruce/globe huckleberry/globe huckleberry  
 2003191 Subalpine fir-Engelmann spruce/globe huckleberry/broom huckleberry  
 200320 Subalpine fir-Engelmann spruce/Rocky Mountain whortleberry  
 2003200 Subalpine fir-Engelmann spruce/Rocky Mountain whortleberry/  
 Rocky Mountain whortleberry  
 2003201 Subalpine fir-Engelmann spruce/Rocky Mountain whortleberry/  
 Jacob's ladder  
 200321 Subalpine fir-Engelmann spruce/broom huckleberry  
 2003210 Subalpine fir-Engelmann spruce/broom huckleberry/broom huckleberry  
 2003211 Subalpine fir-Engelmann spruce/broom huckleberry/whitebarkpine  
 2003212 Subalpine fir-Engelmann spruce/broom huckleberry/Jacob's ladder  
 2003213 Subalpine fir-Engelmann spruce/broom huckleberry/elk sedge  
 2003216 Subalpine fir-Engelmann spruce/broom huckleberry/russet buffaloberry  
 2003217 Subalpine fir-Engelmann spruce/broom huckleberry/heartleaf arnica

200322 Subalpine fir-Engelmann spruce/currant species  
 2003220 Subalpine fir-Engelmann spruce/currant species/currant species  
 2003221 Subalpine fir-Engelmann spruce/currant species/Fendler meadow-rue  
 200323 Subalpine fir-Engelmann spruce/grayleaf willow  
 200324 Subalpine fir-Engelmann spruce/western thimbleberry  
 2003240 Subalpine fir-Engelmann spruce/western thimbleberry/  
 western thimbleberry  
 2003241 Subalpine fir-Engelmann spruce/western thimbleberry/broom huckleberry  
 200325 Subalpine fir-Engelmann spruce/shiny-leaf spirea  
 200326 Subalpine fir-Engelmann spruce/Ross sedge  
 200327 Subalpine fir-Engelmann spruce/Rocky Mountain maple  
 200328 Subalpine fir-Engelmann spruce/pinegrass  
 2003280 Subalpine fir-Engelmann spruce/pinegrass/pinegrass  
 2003281 Subalpine fir-Engelmann spruce/pinegrass/mountain lover  
 200329 Subalpine fir-Engelmann spruce/dwarf bilberry  
 200330 Subalpine fir-Engelmann spruce/mallow ninebark  
 200401 Engelmann spruce/heartleaf arnica  
 200402 Engelmann spruce/elkslip marsh-marigold  
 200403 Engelmann spruce/soft leaved sedge  
 200405 Engelmann spruce-blue spruce/fragrant bedstraw  
 200406 Engelmann spruce/moss species  
 200407 Engelmann spruce/common juniper  
 200408 Engelmann spruce/American twinflower  
 200409 Engelmann spruce/mallow ninebark  
 200413 Engelmann spruce/whiproot clover  
 200414 Engelmann spruce/broom huckleberry  
 2004140 Engelmann spruce/broom huckleberry/broom huckleberry  
 2004141 Engelmann spruce/broom huckleberry/American bistort  
 2004142 Engelmann spruce/broom huckleberry/silvery lupine  
 2004145 Engelmann spruce/broom huckleberry/Jacob's ladder  
 200415 Engelmann spruce/Rocky Mountain whortleberry  
 2004150 Engelmann spruce/Rocky Mountain whortleberry/  
 Rocky Mountain whortleberry  
 2004151 Engelmann spruce/Rocky Mounatin whortleberry/Jacob's ladder  
 200416 Engelmann spruce/Thurber fescue  
 200417 Engelmann spruce-Douglas-fir/common juniper  
 200418 Engelmann spruce/dwarf bilberry

200501 White spruce/sedge  
 200502 White spruce/common juniper  
 200503 White spruce/American twinflower  
 2005030 White spruce/American twinflower/American twinflower  
 2005031 White spruce/American twinflower/broom huckleberry  
 2005032 White spruce/American twinflower/shiny-leaf spirea  
 200601 Blue spruce/Saskatoon serviceberry-redosier  
 2006010 Blue spruce/Saskatoon serviceberry-redosier/Saskatoon serviceberry  
 2006011 Blue spruce/Saskatoon serviceberry-redosier/redosier  
 200602 Blue spruce/heartleaf arnica  
 200603 Blue spruce/bluegrass species  
 200604 Blue spruce-Douglas-fir/American twinflower  
 2006040 Blue spruce-Douglas-fir/American twinflower/American twinflower  
 2006043 Blue spruce-Douglas-fir/American twinflower/common juniper  
 200605 Blue spruce/thinleaf alder  
 200606 Blue spruce-Douglas-fir/silvertop sedge  
 200607 Blue spruce-Douglas-fir/forest fleabane  
 200608 Blue spruce-Douglas-fir/bearberry  
 200609 Blue spruce-Douglas-fir/Arizona fescue  
 2006090 Blue spruce-Douglas-fir/Arizona fescue/Arizona fescue  
 2006091 Blue spruce-Douglas-fir/Arizona fescue/Parry oatgrass  
 200610 Blue spruce-Douglas-fir/Oregon-grape  
 200611 Blue spruce-Engelmann spruce/field horsetail  
 200612 Blue spruce-Douglas-fir/common juniper  
 2006120 Blue spruce-Douglas-fir/common juniper/common juniper  
 2006121 Blue spruce-Douglas-fir/common juniper/elk sedge  
 200701 Whitebark pine/elk sedge  
 2007010 Whitebark pine/elk sedge/elk sedge  
 2007011 Whitebark pine/elk sedge/lodgepole pine  
 200702 Whitebark pine/Ross sedge  
 2007020 Whitebark pine/Ross sedge/Ross sedge  
 2007021 Whitebark pine/Ross sedge/lodgepole pine  
 200703 Whitebark pine-limber pine/varleaf cinquefoil  
 200704 Whitebark pine/Idaho fescue  
 200705 Whitebark pine/common juniper  
 2007050 Whitebark pine/common juniper/common juniper  
 2007051 Whitebark pine/common juniper/buffaloberry

200706 Whitebark pine/broom huckleberry  
 200801 Bristlecone pine/Thurber fescue  
 200802 Bristlecone pine/Arizona fescue  
 200803 Bristlecone pine/whiproot clover  
 200804 Bristlecone pine/mountain gooseberry  
 200805 Bristlecone pine/common juniper  
 200901 Lodgepole pine/bearberry  
 200903 Lodgepole pine/elk sedge  
 2009030 Lodgepole pine/elk sedge/elk sedge  
 2009031 Lodgepole pine/elk sedge/mountain lover  
 200905 Lodgepole pine/common juniper  
 200907 Lodgepole pine/Wheeler bluegrass  
 200908 Lodgepole pine/russet buffaloberry  
 2009080 Lodgepole pine/russet buffaloberry/russet buffaloberry  
 2009081 Lodgepole pine/russet buffaloberry/mountain lover  
 200909 Lodgepole pine/Rocky Mountain whortleberry  
 200910 Lodgepole pine/broom huckleberry  
 200911 Lodgepole pine/Ross sedge  
 200912 Lodgepole pine/dwarf bilberry  
 201001 Limber pine/bluebunch wheatgrass  
 201002 Limber pine/purple pinegrass  
 201003 Limber pine/Idaho fescue  
 201004 Limber pine/spike-fescue  
 2010040 Limber pine/spike-fescue/spike-fescue  
 2010041 Limber pine/spike-fescue/American pasque-flower  
 2010042 Limber pine/spike-fescue/prairie junegrass  
 201005 Limber pine/common juniper  
 201006 Limber pine/whiproot clover  
 201007 Limber pine/curleaf mountain-mahogany  
 201008 Limber pine/creeping juniper  
 201009 Limber pine/Thurber fescue  
 201010 Limber pine/common chokecherry  
 201101 Ponderosa pine-juniper species/bluebunch wheatgrass  
 201102 Ponderosa pine/little bluestem-western wheatgrass  
 201103 Ponderosa pine-juniper species/blue grama  
 201104 Ponderosa pine/sideoats grama  
 201105 Ponderosa pine/elk sedge

2011050 Ponderosa pine/elk sedge/elk sedge  
 2011051 Ponderosa pine/elk sedge/silvery lupine  
 2011052 Ponderosa pine/elk sedge/yellow stonecrop  
 201106 Ponderosa pine/Ross sedge  
 201107 Ponderosa pine/true mountain-mahogany  
 201108 Ponderosa pine/timber oatgrass  
 201109 Ponderosa pine/Arizona fescue  
 2011090 Ponderosa pine/Arizona fescue/Arizona fescue  
 2011091 Ponderosa pine/Arizona fescue/Parry oatgrass  
 2011092 Ponderosa pine/Arizona fescue/blue grama  
 201110 Ponderosa pine/Idaho fescue  
 2011100 Ponderosa pine/Idaho fescue/Idaho fescue  
 2011101 Ponderosa pine/Idaho fescue/greenleaf manzanita  
 201111 Ponderosa pine/spike-fescue  
 201112 Ponderosa pine/common juniper  
 201113 Ponderosa pine/common juniper-common snowberry  
 201115 Ponderosa pine-juniper species/true mountain-mahogany  
 201117 Ponderosa pine-Douglas-fir/mountain muhly  
 2011170 Ponderosa pine-Douglas-fir/mountain muhly/mountain muhly  
 2011171 Ponderosa pine-Douglas-fir/mountain muhly/Fendler ceanothus  
 2011172 Ponderosa pine-Douglas-fir/mountain muhly/thickspike wheatgrass  
 201118 Ponderosa pine/pinyon-Gambel oak  
 201119 Ponderosa pine/mountain ninebark  
 201120 Ponderosa pine/antelope bitterbrush  
 201121 Ponderosa pine/Gambel oak  
 2011210 Ponderosa pine/Gambel oak/Gambel oak  
 2011211 Ponderosa pine/Gambel oak/Arizona fescue  
 2011214 Ponderosa pine/Gambel oak/mountain snowberry  
 2011215 Ponderosa pine/Gambel oak/inland box-elder  
 201122 Ponderosa pine/common chokecherry  
 2011220 Ponderosa pine/common chokecherry/common chokecherry  
 2011221 Ponderosa pine/common chokecherry/silvertop sedge  
 2011222 Ponderosa pine/common chokecherry/Saskatoon serviceberry  
 2011224 Ponderosa pine/common chokecherry/Oregon-grape  
 2011225 Ponderosa pine/common chokecherry/bur oak  
 2011226 Ponderosa pine/common chokecherry/big bluestem  
 201123 Ponderosa pine/shiny spirea

201124 Ponderosa pine/common snowberry  
 2011240 Ponderosa pine/common snowberry/common snowberry  
 2011242 Ponderosa pine/common snowberry/roughleaf ricegrass  
 2011243 Ponderosa pine/common snowberry/Oregon-grape  
 201125 Ponderosa pine/bluebunch wheatgrass  
 2011250 Ponderosa pine/bluebunch wheatgrass/bluebunch wheatgrass  
 2011251 Ponderosa pine/bluebunch wheatgrass/big sagebrush  
 201126 Ponderosa pine/sun sedge  
 201127 Ponderosa pine/blue grama  
 2011270 Ponderosa pine/blue grama/blue grama  
 2011272 Ponderosa pine/blue grama/sand bluestem  
 2011273 Ponderosa pine/blue grama/big sagebrush  
 2011274 Ponderosa pine/Blue grama/pinyon  
 201128 Ponderosa pine/little bluestem  
 2011280 Ponderosa pine/little bluestem/little bluestem  
 2011281 Ponderosa pine/little bluestem/wavyleaf oak  
 201129 Ponderosa pine/greenleaf manzanita  
 2011290 Ponderosa pine/greenleaf manzanita/greenleaf manzanita  
 2011291 Ponderosa pine/greenleaf manzanita/true mountain-mahogany  
 201131 Ponderosa pine/black sagebrush  
 201132 Ponderosa pine/curleaf mountain-mahogany  
 201140 Ponderosa pine/bearberry  
 201150 Ponderosa pine-juniper species/western snowberry  
 201151 Ponderosa pine/bur oak  
 201201 Douglas-fir/Rocky Mountain maple  
 2012010 Douglas-fir/Rocky Mountain maple/Rocky Mountain maple  
 2012011 Douglas-fir/Rocky Mountain maple/mountain lover  
 2012012 Douglas-fir/Rocky Mountain maple/mountain snowberry  
 201202 Douglas-fir/heartleaf arnica  
 2012020 Douglas-fir/heartleaf arnica/heartleaf arnica  
 2012021 Douglas-fir/heartleaf arnica/weedy milkvetch  
 201203 Douglas-fir/Oregon-grape  
 2012030 Douglas-fir/Oregon-grape/Oregon-grape  
 2012032 Douglas-fir/Oregon-grape/common juniper  
 201204 Douglas-fir/Ross sedge  
 201205 Douglas-fir/pinegrass  
 2012050 Douglas-fir/pinegrass/pinegrass

2012052	Douglas-fir/pinegrass/Idaho fescue
2012053	Douglas-fir/pinegrass/ponderosa pine
201206	Douglas-fir/elk sedge
201207	Douglas-fir/true mountain-mahogany
201208	Douglas-fir/Idaho fescue
201209	Douglas-fir/waxflower
201210	Douglas-fir/common juniper
201211	Douglas-fir/mountain lover
201212	Douglas-fir/mallow ninebark
201213	Douglas-fir/mountain ninebark
201214	Douglas-fir/Gambel oak
2012140	Douglas-fir/Gambel oak/Gambel oak
2012141	Douglas-fir/Gambel oak/Arizona fescue
201215	Douglas-fir/shiny-leaf spirea
2012150	Douglas-fir/shiny-leaf spirea/shiny-leaf spirea
2012151	Douglas-fir/shiny-leaf spirea/pinegrass
2012153	Douglas-fir/shiny-leaf spirea/ponderosa pine
201216	Douglas-fir/common snowberry
201217	Douglas-fir/mountain snowberry
2012170	Douglas-fir/mountain snowberry/mountain snowberry
2012171	Douglas-fir/mountain snowberry/Oregon-grape
2012172	Douglas-fir/mountain snowberry/elk sedge
2012173	Douglas-fir/mountain snowberry/spike-fescue
2012174	Douglas-fir/mountain snowberry/bluebunch wheatgrass
201218	Douglas-fir/globe huckleberry
201219	Douglas-fir/bearberry-common juniper
201220	Douglas-fir/greenleaf manzanita
201221	Douglas-fir/antelope bitterbrush
201222	Douglas-fir/Saskatoon serviceberry
201223	Douglas-fir/curleaf mountain-mahogany
201233	Douglas-fir/Arizona fescue
201241	Douglas-fir/ocean spray
201702	Green ash/common chokecherry
210202	Ironwood/succulent hawthorn
210203	Ironwood-bur oak/sparse understory
210301	Narrowleaf cottonwood/Saskatoon serviceberry
2103010	Narrowleaf cottonwood/Saskatoon serviceberry/Saskatoon serviceberry

2103011 Narrowleaf cottonwood/Saskatoon serviceberry/inland box-elder  
 210302 Narrowleaf cottonwood/sandbar willow-river birch  
 210303 Narrowleaf cottonwood/river birch-currant species  
 210304 Narrowleaf cottonwood/mountain ninebark-common chokecherry  
 210305 Narrowleaf cottonwood-Engelmann spruce/bush honeysuckle  
 210306 Narrowleaf cottonwood/thinleaf alder-redosier  
 210401 Plains cottonwood/western snowberry-giant wildrye  
 2104010 Plains cottonwood/western snowberry-giant wildrye/western snowberry  
 2104011 Plains cottonwood/western snowberry-giant wildrye/redosier  
 210402 Plains cottonwood-narrowleaf cottonwood/willow species  
 210403 Plains cottonwood/willow species  
 210404 Plains cottonwood/American black currant  
 210405 Plains cottonwood/western snowberry-sandbar willow  
 210501 Quaking aspen/elk sedge  
 210502 Quaking aspen/beaked hazel  
 2105020 Quaking aspen/beaked hazel/beaked hazel  
 2105021 Quaking aspen/beaked hazel/bracken  
 2105022 Quaking aspen/beaked hazel/wild sarsaparilla  
 210503 Quaking aspen/Thurber fescue  
 210504 Quaking aspen/common cow-parsnip  
 210505 Quaking aspen/aspen peavine  
 210507 Quaking aspen/silvery lupine  
 210508 Quaking aspen/common juniper  
 210510 Quaking aspen/bracken  
 210511 Quaking aspen/mountain snowberry  
 210512 Quaking aspen/Fendler meadow-rue  
 2105120 Quaking aspen/Fendler meadow-rue/Fendler meadow-rue  
 2105121 Quaking aspen/Fendler meadow-rue/golden banner  
 2105123 Quaking aspen/Fendler meadow-rue/stinging nettle  
 210513 Quaking aspen/false-hellebore  
 210514 Quaking aspen/big sagebrush  
 210515 Quaking aspen/Saskatoon serviceberry  
 2105150 Quaking aspen/Saskatoon serviceberry/Saskatoon serviceberry  
 2105151 Quaking aspen/Saskatoon serviceberry/Rocky Mountain maple  
 2105152 Quaking aspen/Saskatoon serviceberry/Gambel oak  
 2105153 Quaking aspen/Saskatoon serviceberry/Engelmann aster  
 2105154 Quaking aspen/Saskatoon serviceberry/balsam poplar

210516 Quaking aspen/sticky-laurel  
 210517 Quaking aspen/pinegrass  
 210518 Quaking aspen/lovage species  
 210519 Quaking aspen/common chokecherry  
 2105190 Quaking aspen/common chokecherry/common chokecherry  
 2105191 Quaking aspen/common chokecherry/common snowberry  
 210520 Quaking aspen/Oregon-grape  
 210521 Quaking aspen/bearberry  
 210522 Quaking aspen/Arizona fescue  
 210523 Quaking aspen/black elderberry  
 210601 Bur oak/western snowberry  
 2106010 Bur oak/western snowberry/western snowberry  
 2106011 Bur oak/western snowberry/quaking aspen  
 210603 Bur oak/hazelnut species  
 210701 Green ash/western snowberry  
 2107010 Green ash/western snowberry/western snowberry  
 2107011 Green ash/western snowberry/prairie sandreed  
 2107020 Green ash/common chokecherry/common chokecherry  
 2107021 Green ash/common chokecherry/Sprengel's sedge  
 210801 Paper birch/beaked hazel  
 210901 Balsam poplar/redosier  
 212051 Douglas-fir/pinegrass/mountain lover  
 220101 Oneseed juniper/sideoats grama  
 220102 Oneseed juniper/blue grama  
 220103 Oneseed juniper/western wheatgrass  
 220201 Pinyon-Utah juniper/beardless bluebunch wheatgrass  
 220202 Utah juniper/big sagebrush  
 220203 Utah juniper/true mountain-mahogany-squaw-apple  
 2202030 Utah juniper/true mountain-mahogany-squaw-apple/  
 true mountain-mahogany  
 2202031 Utah juniper/true mountain-mahogany-squaw-apple/  
 Wyoming big sagebrush  
 220204 Utah juniper/Indian ricegrass  
 220205 Utah juniper/yellow-wood  
 220206 Utah juniper/Salina wildrye  
 220301 Rocky Mountain juniper/western wheatgrass  
 220302 Rocky Mountain juniper/big sagebrush

220303 Rocky Mountain juniper/bluebunch wheatgrass  
220304 Rocky Mountain juniper/true mountain-mahogany  
220306 Rocky Mountain juniper/antelope bitterbrush  
220307 Rocky Mountain juniper/little ricegrass  
220401 Pinyon-Utah juniper/big sagebrush  
2204010 Pinyon-Utah juniper/big sagebrush/big sagebrush  
2204011 Pinyon-Utah juniper/big sagebrush/blue grama  
220402 Pinyon/blue grama  
220403 Pinyon-Utah juniper/Utah serviceberry-true mountain-mahogany  
2204030 Pinyon-Utah juniper/Utah serviceberry-true mountain-mahogany/  
Utah serviceberry  
2204031 Pinyon-Utah juniper/Utah serviceberry-true mountain-mahogany/  
greenleaf manzanita  
220404 Pinyon/Gambel oak  
220405 Pinyon-Utah juniper/antelope bitterbrush  
220406 Pinyon-Utah juniper/muttongrass  
220407 Pinyon-oneseed juniper/true mountain-mahogany  
220408 Pinyon-oneseed juniper/Nelson's needlegrass  
220409 Pinyon-Utah juniper/true mountain-mahogany  
2204090 Pinyon-Utah juniper/true mountain-mahogany/true mountain-mahogany  
2204091 Pinyon-Utah juniper/true mountain-mahogany/Gambel oak  
220410 Pinyon/black sagebrush

**APPENDIX B: REGION 3 PLANT ASSOCIATION CODES FOR THE  
CENTRAL ROCKIES VARIANT**

3001010	White fir/Rocky Mountain maple
3001011	Oregongrape phase
3001012	Rockspirea phase
3001013	Riparian phase
3001020	White fir/Oregongrape
3001021	New Mexico Locust phase
3001022	Common juniper phase
3001030	White fir/sprucefir fleabane
3001040	White fir/Arizona fescue
3001041	Muttongrass phase
3001042	Gambel oak phase
3001050	White fir/Gambel oak
3001051	Screwleaf muhly phase
3001052	Arizona fescue phase
3001053	Pine muhly phase
3001054	Rockspirea phase
3001060	White fir/Screwleaf muhly
3001070	White fir/Arizona peavine
3001080	White fir/Bigtooth maple
3001081	Rockspirea phase
3001090	White fir/Kinnikinnik
3001100	White fir/Whortleberry
3001110	White fir/New Mexico locust
3001111	Dryspike sedge phase
3001120	White fir/Beardless wildrye
3001130	White fir/Arizona walnut
3001140	White fir/whortleleaf snowberry ponderosa pine series
3001141	Limber pine phase
3001150	White fir/dryspike sedge
3001160	White fir/burnet ragwort
3003	Abies bifolia (corkbark fir)
3003060	Corkbark fir/mountain bluebells
3003080	Corkbark fir/sprucefir fleabane

3003090	Subalpine fir/common juniper
3003110	Corkbark fir/Moss
3003111	Engelmann spruce phase
3003112	Douglas-fir phase
3003200	Corkbark fir/Whortleberry
3003201	Twinflower phase
3003202	Thimbleberry phase
3003203	Cliffbrush phase
3003231	Rocky Mountain maple Phase
3003240	Corkbark fir/Thimbleberry
3003300	Corkbark fir/Burnet ragwort
3003301	Douglas-fir phase
3003310	Corkbark fir/Arizona peavine
3003320	Corbark fir/cliffbush
3003350	Corkbark fir/scree
3003370	Corkbark fir/dryspike sedge
3004060	Engelmann spruce/Moss typic phase
3004061	Typical phase
3004062	Interior Douglas-fir phase
300415	Engelmann spruce/Whortleberry-skunkweed polemonium
3004151	Engelmann spruce phase
3004152	Corkbark fir phase
3004300	Engelmann spruce/Rocky Mountain maple
3004310	Engelmann spruce/Sprucefir fleabane
3004320	Engelmann spruce/beardless wildrye
3004330	Engelmann spruce/Ross avens
3004340	Engelmann spruce/gooseberry currant
300435	Engelmann spruce/bittercress ragwort
3004350	Corkbark phase
3004351	White fir phase
3004360	Engelmann spruce/Whortleberry
3006010	Blue spruce/Redosier dogwood
300604	Blue spruce/Twinflower
3006060	Blue spruce/Dryspike sedge
3006070	Blue spruce/Sprucefir fleabane
3006071	Ponderosa pine phase
3006080	Blue spruce/Kinnikinnik

3006090	Blue spruce/Arizona fescue
3006130	Blue spruce/bittercress ragwort
3011	Picea pungens (blue spruce)
3011030	Ponderosa pine/blue grama
3011031	Little bluestem phase
3011032	Sand bluestem phase
3011033	Big sagebrush phase
3011034	Gray oak phase
3011035	Gambel oak phase
3011090	Ponderosa pine/Arizona fescue phase
3011091	Parry danthonia phase
3011092	Blue grama phase
3011093	Gambel oak phase
3011130	White fir/scree
3011210	Ponderosa pine/Gambel oak
3011211	Arizona fescue phase
3011212	Longtongue muhly phase
3011213	Twoneedle pinyon phase
3011214	Mountain muhly phase
3011215	Blue grama phase
3011216	New Mexico locust phase
3011220	Ponderosa pine/Silverleaf oak
3011320	Ponderosa pine/Stansbury cliffrose
3011330	Ponderosa pine/mountain muhly
3011340	Ponderosa pine/screwleaf muhly
3011341	Gambel oak phase
3011350	Ponderosa pine/Indian ricegrass
3011360	Ponderosa pine/Gray oak /mountain muhly phase
3011361	Longtongue muhly phase
3011370	Ponderosa pine/wavyleaf oak
3011380	Ponderosa pine/black sagebrush
3011390	Ponderosa pine/screwleaf muhly -Arizona fescue
3011391	Blue grama phase
3011392	Gambel oak phase
3011400	Ponderosa pine/kinnikinnik
3011410	Ponderosa pine/Arizona white oak
3011411	Blue grama phase

3011420 Ponderosa pine/pointleaf manzanita c. t.  
 3011430 Ponderosa pine/netleaf oak  
 3011440 Ponderosa pine/Emory oak  
 3011460 Ponderosa pine/scree  
 3011470 Ponderosa pine/Arizona walnut  
 3011500 Ponderosa pine/rockland  
 301203 Douglas-fir/Oregongrape  
 301213 Douglas-fir/mountain ninebark  
 3012140 Douglas-fir/Gambel oak  
 3012141 Arizona fescue phase  
 3012142 Screwleaf muhly phase  
 3012143 Rockspirea phase  
 301231 Douglas-fir/kinnikinnik  
 3012320 Douglas-fir/fringed brome  
 3012330 Douglas-fir/Arizona fescue  
 3012331 Bristlecone pine phase  
 3012332 Limber pine phase  
 3012333 Aspen phase  
 3012340 Douglas-fir/Mountain muhly / pinyon pine phase  
 3012341 Limber pine phase  
 3012350 Douglas-fir/screwleaf muhly  
 3012360 Douglas-fir/Silverleaf oak ponderosa pine phase  
 3012361 Chihuahua pine phase  
 3012362 Netleaf oak phase  
 3012380 Douglas-fir/scree  
 301239 Douglas-fir/bigtooth maple  
 301241 Douglas-fir/rockspirea  
 301242 Douglas-fir/wavyleak oak  
 3012430 Douglas-fir/Arizona white oak  
 303101 Arizona cypress/silverleaf oak  
 303102 Arizona cypress/shrub live oak  
 3032010 Apache pine/longtongue muhly  
 3032030 Apache pine/silverleaf oak  
 3033010 Chihuahua pine/pinyon ricegrass  
 3033020 Chihuahua pine/Arizona white oak  
 3033030 Chihuahua pine/Silverleaf oak  
 3103 Populus angustifolia (narrowleaf cottonwood)

3104 Populus deltoides spp. wislizeni (Rio Grande cottonwood)  
 3123 Alnus tenuifolia (thinleaf alder)  
 3130 Platanus wrightii (Arizona sycamore)  
 3201010 Oneseed juniper/sideoats grama  
 3201011 Beargrass phase  
 3201020 Oneseed juniper/blue grama  
 3201040 Oneseed juniper/big sagebrush  
 3201331 Oneseed juniper/Rabbitbrush-Apacheplume  
 3201332 Big sagebrush phase  
 3201333 Gray oak phase  
 3201340 Oneseed juniper/sand bluestem  
 3201350 Oneseed juniper/Bigelow sagebrush  
 320140 Oneseed juniper/winterfat  
 3201400 Oneseed juniper/wavyleaf oak  
 3201410 Oneseed juniper/sacahuista-lecheguilla  
 3201420 Oneseed juniper/lecheguilla  
 3201430 Pinchot juniper/creosotebush  
 3202020 Utah juniper/big sagebrush  
 3202320 Utah juniper/blue grama  
 3202321 Cliffrose phase  
 3202330 Utah juniper/tobosagrass mesquite phase  
 3202331 Arizona pinyon phase  
 3202500 Utah Juniper-oneseed juniper/sparse c.t.  
 3204010 Twoneedle pinyon pine/big sagebrush Utah juniper phase  
 3204011 Oneseed juniper phase  
 3204012 Rocky Mountain juniper phase  
 3204021 Twoneedle pinyon pine/blue gama Utah juniper phase  
 3204022 Oneseed juniper phase  
 3204023 Alligator juniper phase  
 3204024 Hillslope phase  
 3204031 Twoneedle pinyon pine/treu mountain mahogany wavyleaf oak phase  
 3204032 Gray oak phase  
 3204033 Gambel oak phase  
 320404 Twoneedle pinyon pine/Gambel oak  
 3204050 Twoneedle pinyon pine/antelope bitterbrush  
 320406 Twoneedle pinyon pine/Muttongrass  
 320410 Twoneedle pinyon pine/pine muhly

320411 Twoneedle pinyon pine/New Mexico muhly  
 3204300 Twoneedle pinyon pine/sand bluestem  
 320431 Twoneedle pinyon pine/Arizona fescue  
 3204320 Twoneedle pinyon pine/Stansbury cliffrose  
 3204321 Big sagebrush phase  
 3204330 Twoneedle pinyon pine/Rabbitbrush-Apacheplume  
 3204350 Twoneedle pinyon pine/rockland  
 3204360 Twoneedle pinyon pine/wavyleaf oak  
 3204370 Twoneedle pinyon pine/Dore needlegrass  
 3204400 Twoneedle pinyon pine/manzanita  
 320441 Twoneedle pinyon pine/blackbrush  
 3204500 Twoneedle pinyon pine/sparse c. t.  
 3230030 Redberry juniper/crucifixion thorn  
 3230040 Redberry juniper/shrub live oak shrub live oak phase  
 3230041 Mesquite phase  
 3230042 Blue grama phase  
 3231010 Alligator juniper/pointleaf manzanita  
 3231020 Alligator juniper/blue grama  
 3231021 Mesquite phase  
 3231030 Alligator juniper/desert ceanothus  
 3231040 Alligator juniper/skunkbush sumac  
 3231050 Alligator juniper/Bullgrass  
 3232020 Border pinyon/Mexican orange  
 3232030 Border pinyon/bullgrass  
 323204 Border pinyon/pinyon ricegrass  
 3232050 Border pinyon/Toumey oak  
 3232060 Border pinyon/silverleaf oak  
 3232070 Border pinyon/evergreen sumac  
 3232330 Border pine/Rabbitbrush-Apacheplume  
 3233010 Arizona pinyon pine/manzanita  
 3233020 Arizona pinyon pine/blue grama alligator juniper phase  
 3233021 Utah juniper phase  
 3233022 Cliffrose phase  
 3233030 Arizona pinyon pine/crucifixion thorn  
 3233040 Arizona pinyon/shrub live oak vegetation  
 3233041 Typic phase  
 3233042 Cliffrose phase

3233050	Arizona pinyon pine/banana yucca
3233330	Arizona pinyon/Rabbitbrush-Apacheplume
3238040	Bristlecone pine/Gooseberry current
3238300	Bristlecone pine/Arizona fescue
3238310	Bristlecone pine/Thurber fescue
3240300	Limber pine/Kinnikinnik
325000	Scarp Woodland
3335	Salix bebbiana (Bebb willow)
3610010	Mexican blue oak/mixed grama
3610020	Mexican blue oak/common sotol
3620010	Emory oak/pointleaf manzanita
3620020	Emory oak/sideoats grama
3620021	Sacahuista phase
3620030	Emory oak/common sotol
3620040	Emory oak/Arizona walnut
3630010	Gray oak/sideoats grama
3630020	Gray oak/true mountain mahogany
3630030	Arizona white oak/bullgrass
3630040	Arizona white oak/skunkbush sumac
3630041	Alligator juniper phase
3630042	Oneseed juniper phase
3630043	Pinyon ricegrass phase
3630050	Arizona white oak/pinyon ricegrass
3650010	Silverleaf oak/longtongue muhly